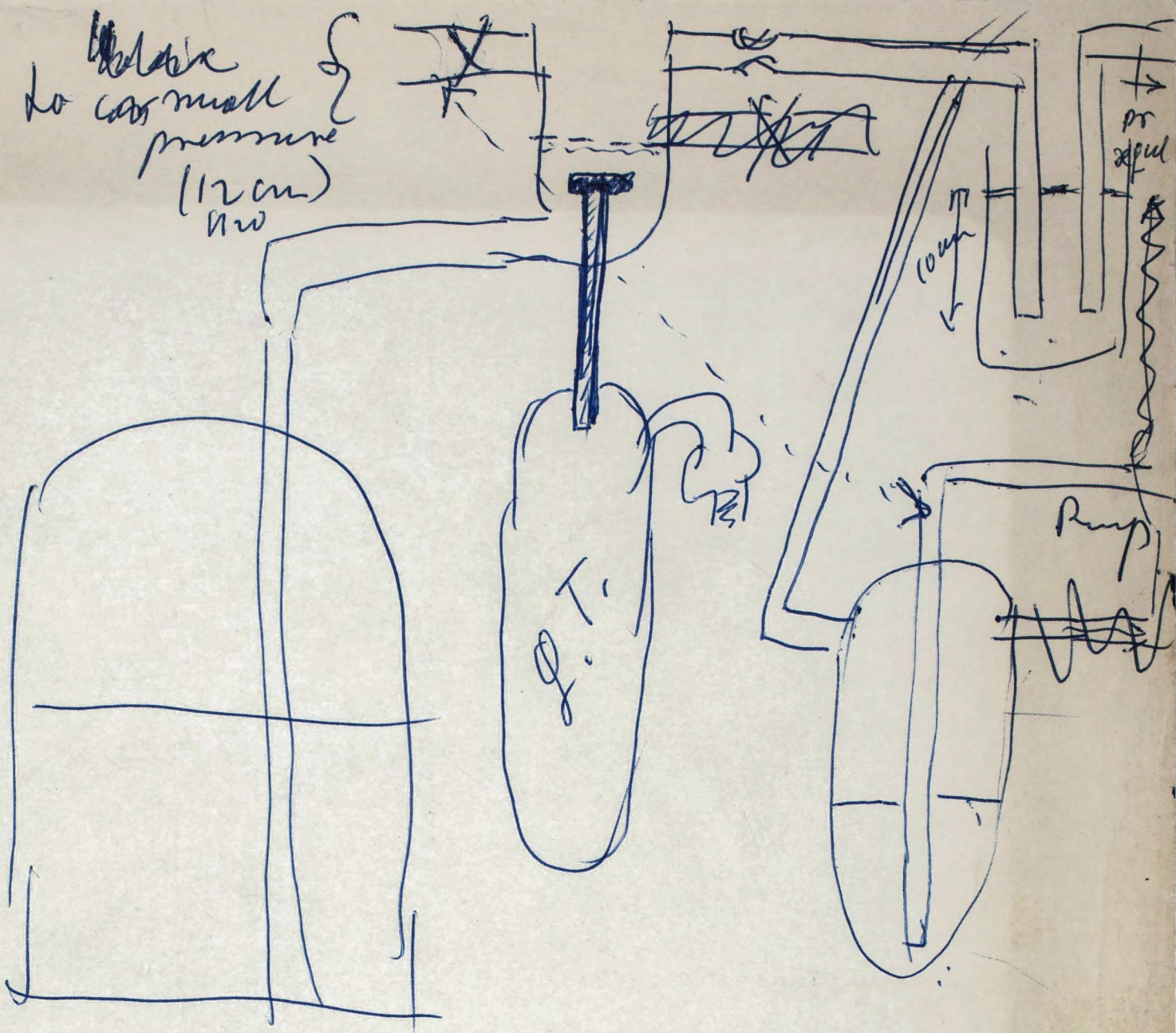


to ~~the~~ ^{the} small
pressure
(12 cm)
H₂O



- B/r is +

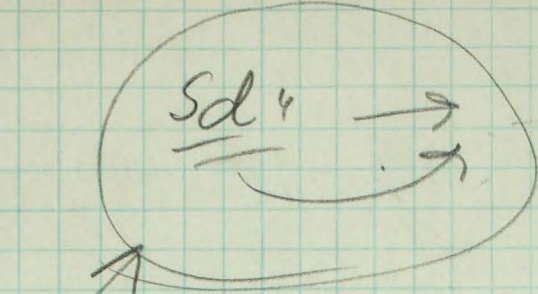
1 in 10^4 is negative [natural]
1 in 10^2 is negative. [UV] 10^4 improved

subtle)
natural whole (culture).
after U.V. restored
~~after~~

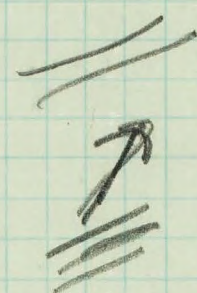
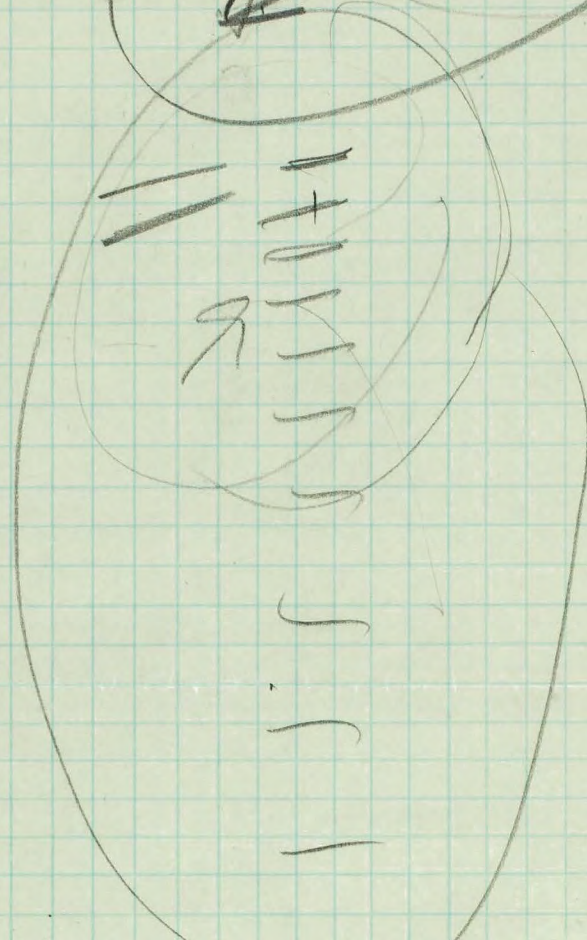
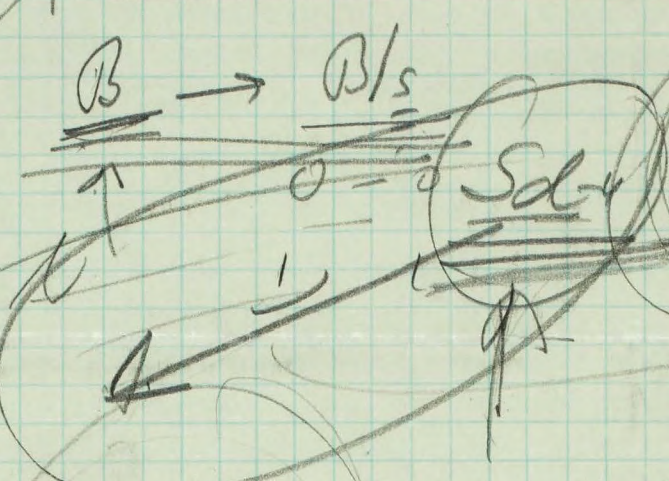
12:30
munch

~~the~~ tubes unfused





Sd-4 10⁸
 ↓ 10⁴



10⁸
52^o
2 - 279

ferrous
many

0.02%

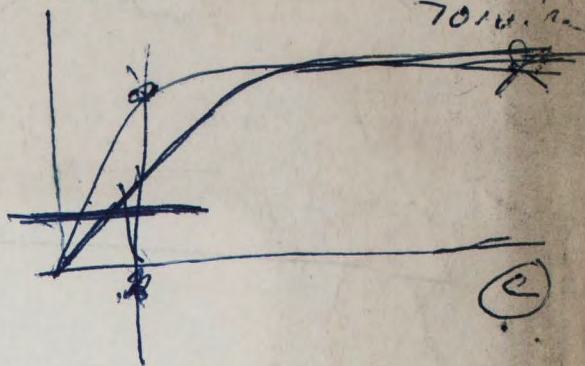
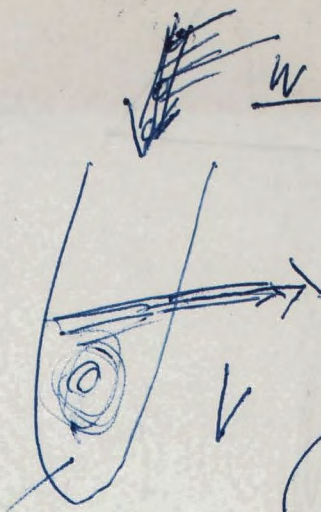
0.02 gm in 100 cc
 60 min

1800 mutants / 10⁸

ferrous 5 min
 0.025 gm / 100 cc
 52^o / 100 mutants

180 / mutants / 10⁸ Strict independence

75

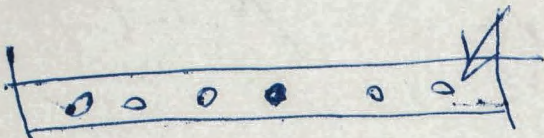


$$\frac{w}{v}$$

> 70

700

$$e^{-\frac{w}{v}t}$$

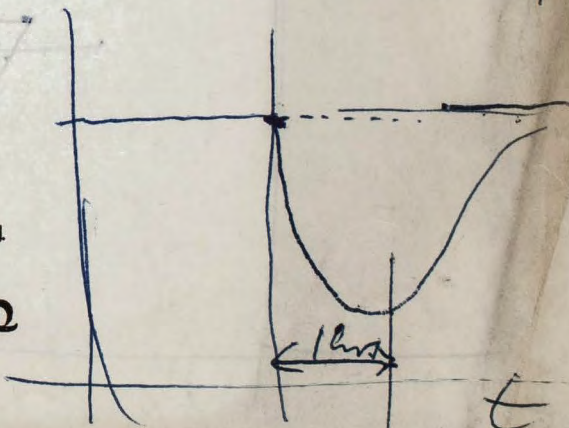
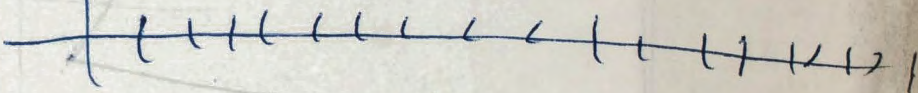
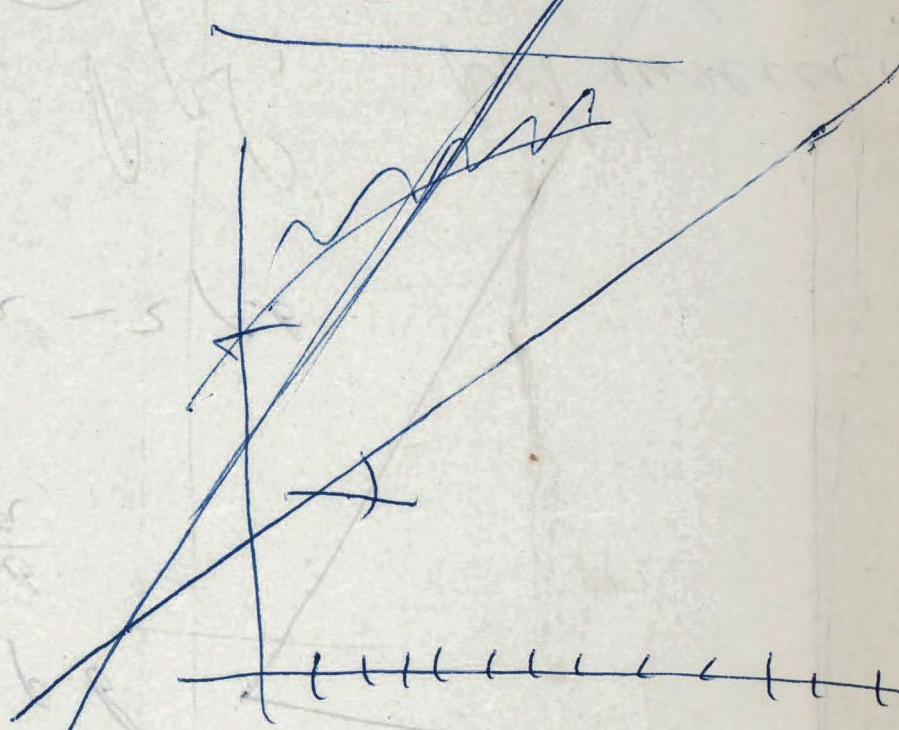


$\frac{2\pi}{\lambda}$

2.5 10

7.5 10

15 10



$$\frac{dy}{dt} = a$$

$$\frac{dy}{dt} = \rho b$$

$$\frac{dy}{dt} = a - \rho b$$

$$\rho = \frac{b}{a}$$

$$\frac{dy}{dt} = 2a - 2\rho b$$

Engel P.P.

Art Museum.

Dept of

Quadrangle

Raphael Kurzrok

Thomas Park

Transfile E

① of 8

- ① "1950 Paper" Chomostat Biology ~~File~~ Dittos.
Several versions. Preprint.
- ② Notebook - lab books.
Clipping. Denver Post, Jan 21, 1951
LS Joined U. Colo. Med. School. Visiting Prof. Biophysics
"Algae - 1950" Also Dec 1950.
Memorandum on growing Photosynthetic
Organisms in Sunlight & Daylight. Jan 19, 1951
Typed paper, never published.
- 3) Microbial Genetics Bulletin. #6. April 1952.
Cold Spring Harbor.
- 4) Cold Spring Harbor course Notebook. Aug. ?
Laboratory Manual, 1947. Bacteriophage
- 5) "Microscopes." ^{by DeBrock & Adams} 1953. equipment catalogs.
- 6) Biology. Freezing ^{of bull sperm} 1952. (with Fox)
- 7) Biology Bull sperm freezing, Biology low temperature.
Data, 1953. Includes bibliography. Photos
- 8) "Aging" Calculations
- 9) "Age". Notebook with calculations.
References & notes.

"Fan"
Stalin letter

E

(2)

10)

Clipping Wash. Post. 11/25/47.

"Scientists' Appeal to Stalin Balked"

Includes letter from school children + answer
by L.S.

Christmas cards 1947.

Correspondence re Stalin from public.

11)

~~Biology Notes~~ "Library" ^{biological} References.

Includes list of books borrowed from biology library

12)

Misc. Found loose.

Some bio notes. Reprints. Abstracts
Removed, Remembered E-40

Asynchronous
Means ^{to} Palter

Dr. Nisrowsky

269

U_t searched up to $t = t$

$$\frac{dU}{dt} = k_u C$$

$$-\frac{dC}{dt} = k_T C + k_{univ} C$$

$$-(k_T + k_u) t$$

$$C = \frac{C_0 C}{k_T + k_u}$$

$$\frac{dU}{dt} = \frac{k_u C_0 C}{k_T + k_u} \quad -(k_T + k_u) t$$

0.05 around

0.12

0.1 - 0.3

25

microcosm

100 groups
of hydro
radice

0.01 mgm } in leaf

24 grains = 6.5 gm

1 grain = 0.06 gm = 60 mgm

(400)

$$\ln \frac{dL}{dt} = \ln \frac{K_u C_0}{K_d + K_u} - (K_d + K_u) t$$

Hydrocodone 200 mg tablet
 strength 0.23%

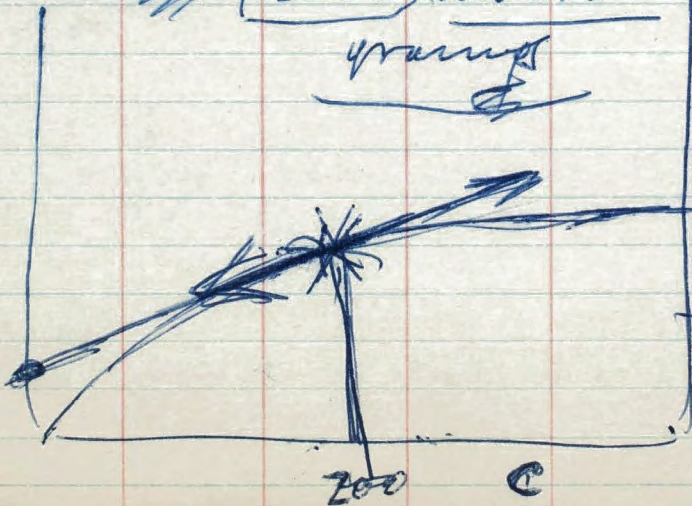
$$200 \times \frac{2}{1000}$$

$\frac{4}{10}$ mgm J

Mecams
 page 66

comp 0.2 mgm
 per mg

$\frac{200}{1000}$ mgm



20 to 80 mgm
 grams
 per day

Pack of 108

1.3%

1 cc = 13 mgm

65 times
 daily require 1.3 gm
 must 100 gm

$\frac{1.3}{100} \times 100$ gm in 100 cc

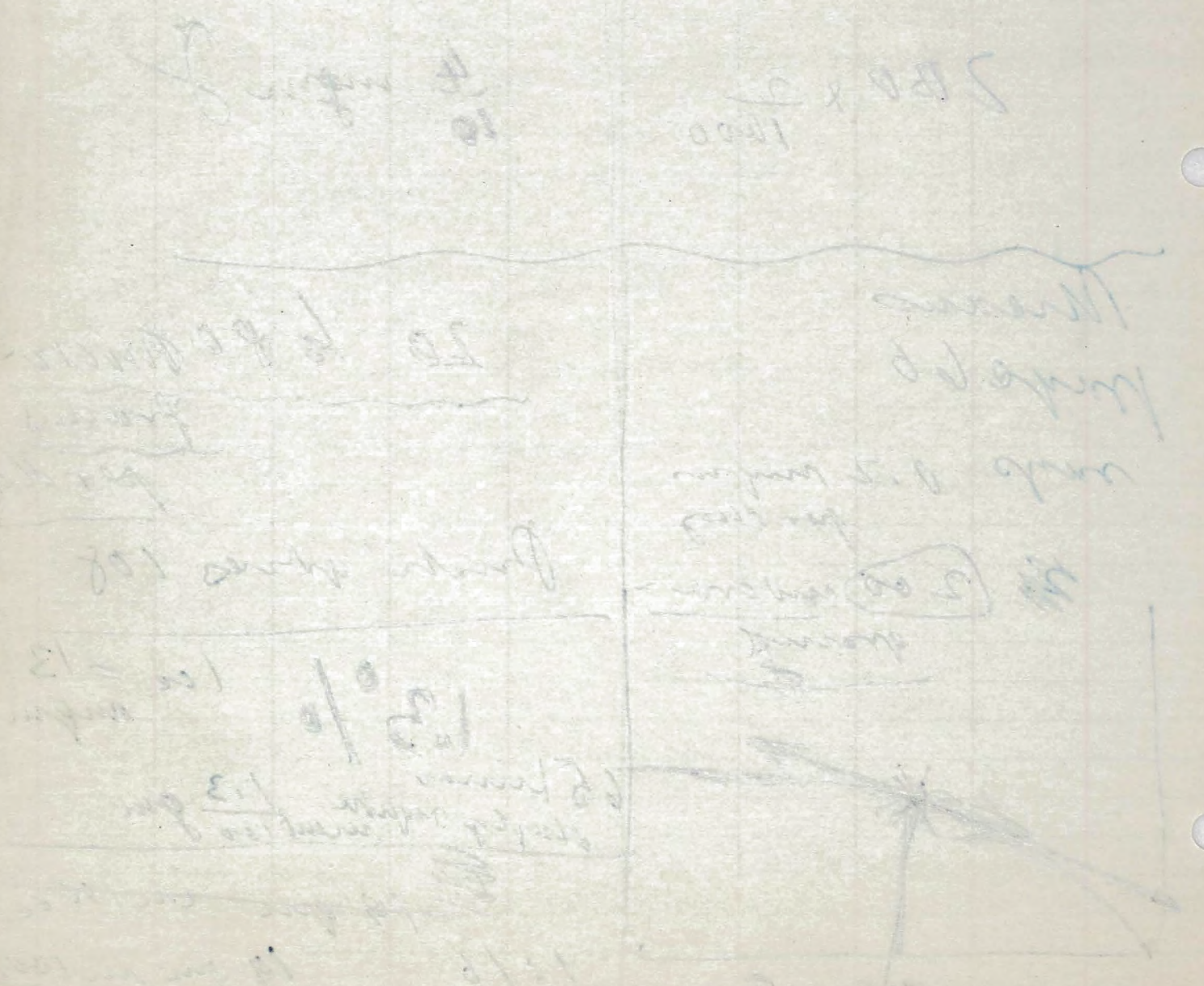
1:16

19 gm in 100 cc

Yeastized salt [1 part of yeast
to 10 of salt]

Silber man (2 quarts per day)
15 to 40 g/day = 200 g/day

minimum requirement



Der Lohschell

unwichtig
 $f(n) f(n) f(n+1)$

das gleiche
 hand



$e^{-\beta n}$

$\frac{df(n)}{dt} = [f(n) e^{-\beta n}] \frac{d}{dt} - k f(n)$

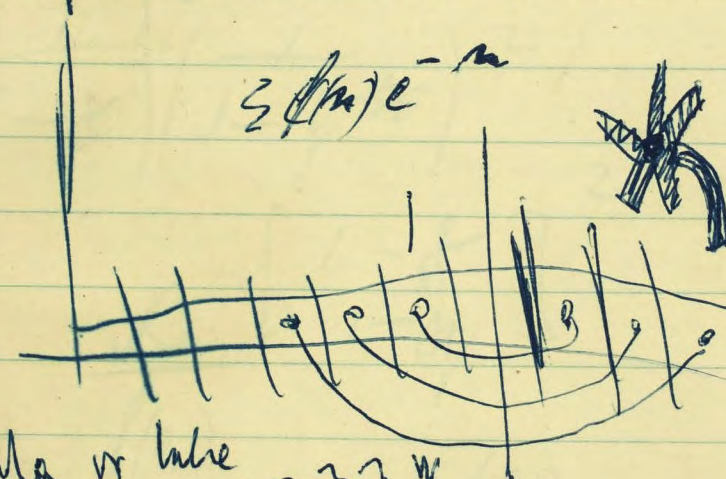
$\frac{df(n)}{dt} = \bar{a} f(n) - k f(n)$

$\sum_{k=0}^n (f(n-k) f(n+k) - f(n,0) k + k f(n-1) - k f(n) = \bar{a} f(n)$

$f(n) = \dots f^n$

$f^{n-k} f^{n+k} e^{-\beta n}$

unwichtig



$\sum f(n) e^{-\beta n}$

N total number

$\frac{f(0)}{N} - k f(0) = \bar{a} f(0)$

$\frac{df(n)}{dt} = \bar{a} f(n)$

Ma or lake
 5101

$\frac{f(n)}{f(n-1)}$

$f(0) - k = \bar{a}$

$$f(t) = \sum_{i,k} f(i) f(k) e^{-(i+k)\beta} e^{-i+k}$$

$$f^i f^k$$

$$f^{i+k} e^{-(i+k)\beta} e^{-i+k}$$

$$\sum_{i,k} \left[\frac{f e^{-(i+k)\beta}}{e^{i+k}} \right] e^{-i+k} = f(t)$$

$$\sum_{i,k} \left(\frac{f}{e^{i+k}} \right)^{i+k}$$

$$1 + q + q^2 + q^3 \dots$$

$$\sum_{i,k} A^{i+k}$$

$$A [A^0 + A^1 + A^2 + \dots] = A \left[\frac{1}{1-q} \right]$$

$$+ A^2 [$$

$$A^3 [\dots]$$

$$\left(\frac{1}{1-q} \right)^2 \left(\frac{1}{1-q} \right)^2$$

$$\left(\frac{1}{1-q} \right)^2 \sum_{i,k} q = \left(\frac{f}{e^{i+k}} \right)^2$$

$$\frac{d}{dt} \left[\frac{1-f}{1-q} \right]^2$$

$$\left(\frac{1}{1 - \frac{f}{e^{i+k}}} \right)^2 = f(t)$$

$$\left(\frac{f(t)}{\frac{f(t)}{A} - \frac{1}{A} \frac{1}{e^{i+k}}} \right)^2 = f(t)$$

$$r = \frac{f(t)}{\frac{f(t)}{A} - \frac{1}{A} \frac{1}{e^{i+k}}}$$

~~$$1 = \frac{f(0)}{k - r \frac{1}{e^{(1+r)}}$$~~

~~$$f(0) - k e^{-((1+r))} = f(0)$$~~

~~$$1 = k e^{-((1+r))}$$~~

~~$$k = e^{(1+r)}$$~~

$$\bar{a} = \frac{1}{10}$$

$$\frac{k}{1+r} < 1$$

$$k < 1+r$$

$$\frac{k}{\bar{a}+k} < 1$$

$$k \leq f(0)$$

$$\frac{f(0)}{[f(0) - k e^{-((1+r))}]^2} = 1$$

$$f(0) = f(0)^2 - 2k e^{-((1+r))} f(0) - k^2 e^{-2((1+r))}$$

$$0 = f(0) - [2k e^{-((1+r))} + 1] k e^{-2((1+r))}$$

$$0 = 1 - [2k e^{-((1+r))} + 1] \frac{k}{f(0)} e^{-2((1+r))}$$

$$\frac{1-f}{B} = \bar{a} + k$$

$$\frac{k}{\bar{a}+k} = f$$

$$1 - \frac{1}{\bar{a}+k} = B(\bar{a}+k)$$

$$\bar{a} + k = B(\bar{a}+k)^2$$

$$\left[\frac{1-f}{1 - \frac{k}{e^{1+r}}} \right]^2 = \frac{(1-f) e^{1+r}}{e^{1+r} - k} (\bar{a} + k) f$$

Effect of more than one offspring (m)

$$\Delta f(n) = m f(n) e^{-\beta n} + \lambda m e^{-\beta(n-1)} - \lambda m e^{-\beta n}$$

($f(n)$ number of bushes with born with n mutations in them in k generations

$\Delta f(n)$ increase in $k+1$ generations

$$\Delta f(n) = \bar{a} f(n)$$

$$\bar{a} f(n) = m f(n) e^{-\beta n} + \lambda m e^{-\beta(n-1)} - \lambda m e^{-\beta n}$$

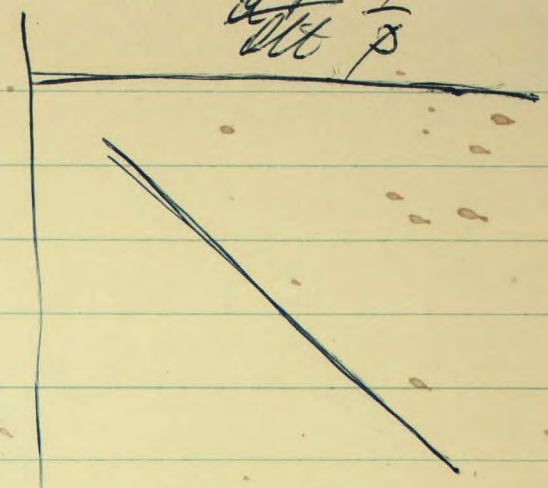
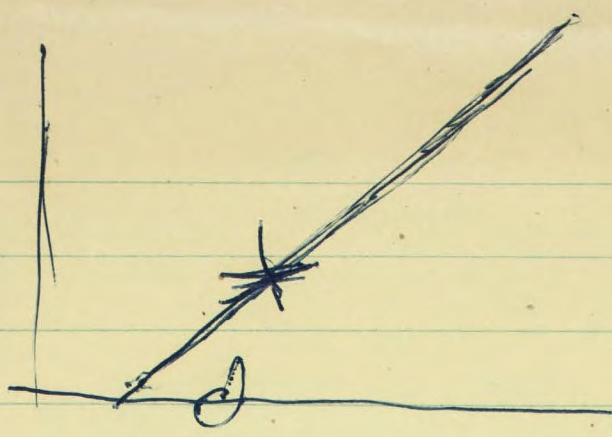
$$e^{\beta n} \bar{a} f(n) = m f(n) + \lambda m f(n)$$

$$\bar{a} + \lambda m = m$$

$$(\bar{a} - m e^{-\beta n} + \lambda m) f(n) = \lambda m e^{-\beta(n-1)} f(n)$$

$$\frac{f(n)}{f(n-1)} = \frac{\lambda m e^{\beta} e^{-\beta n}}{\bar{a} - m e^{\beta n} + \lambda m} = \frac{\lambda e^{\beta} e^{-\beta n}}{1 - e^{-\beta n}}$$

SP 1/8



Katkov in → Phys Chem
for background →

Rehberg Physiology

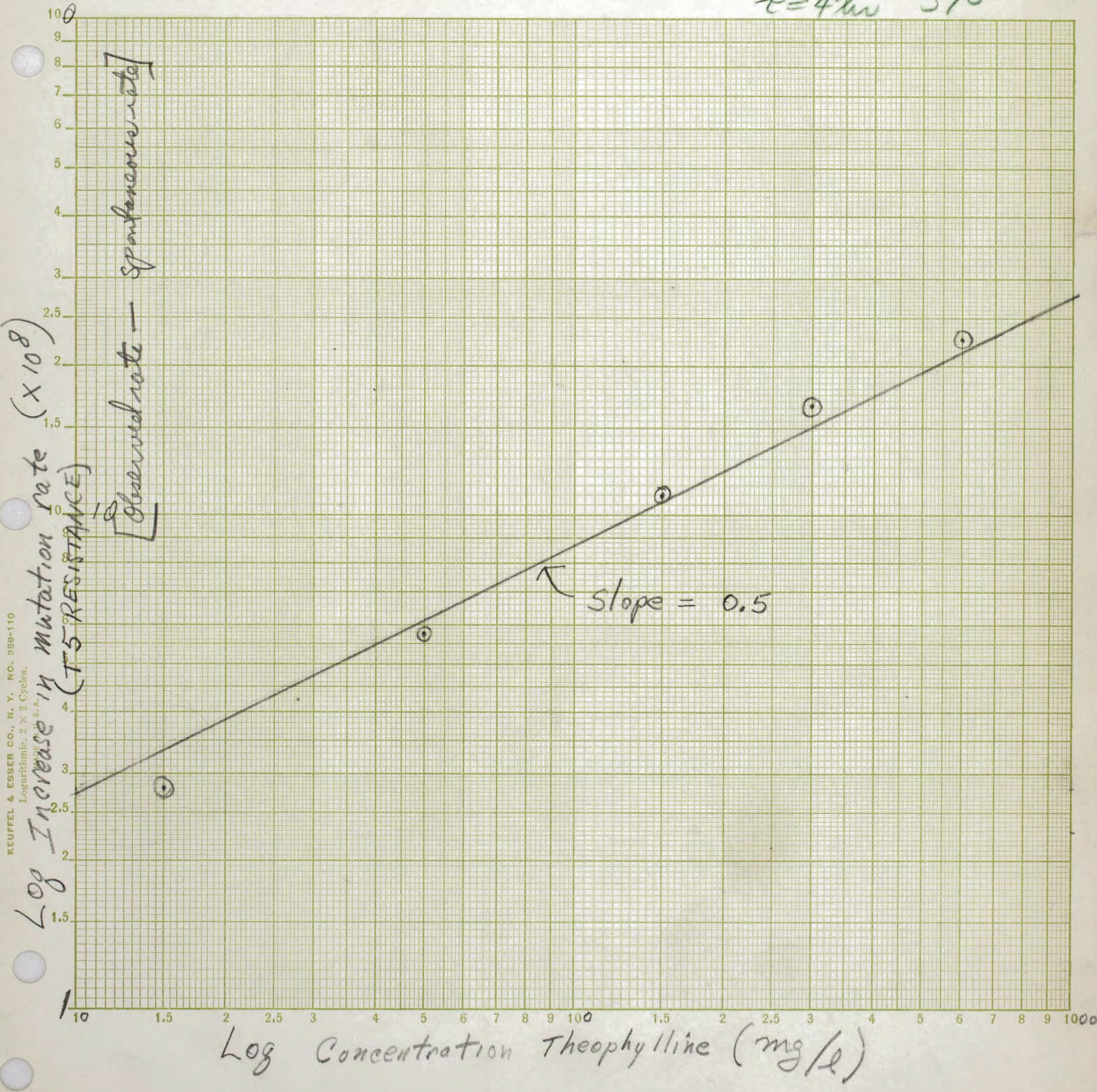
~~Carl~~
Schubert's lung & Carlsberg
Halper
~~Anders~~

Fischer Pathological dust
of the lungs Lungenkrankheiten

Wernicke's dust. Frickhoffer
→ Pinner's (Chem. (Kunststoff)
Körperbau
Körperbau
Körperbau

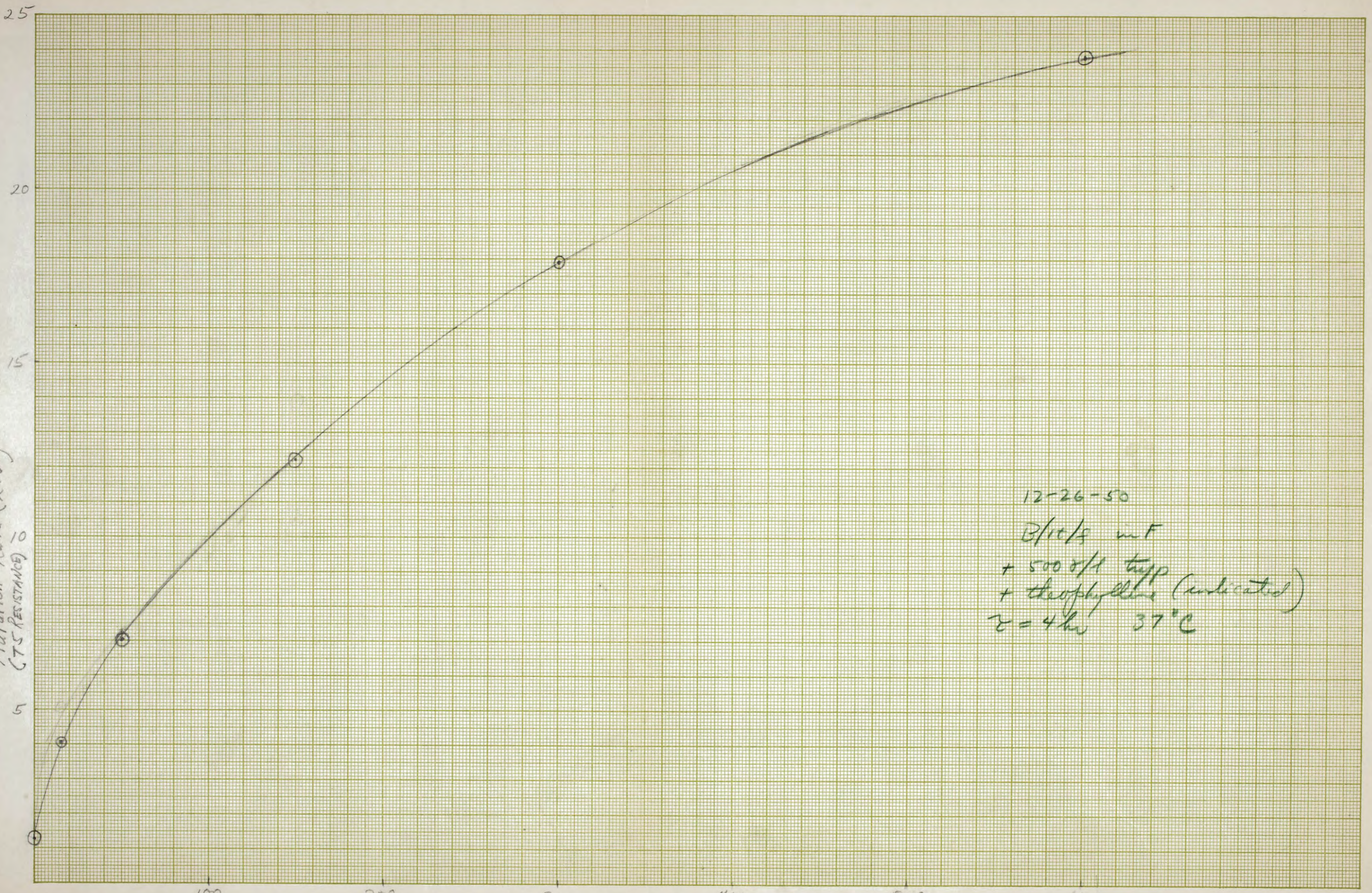
Herbstadius exp. of dust.
See Anthon. 1844

12-26-50
 B/10/min +
 + 5005/l trypt
 + theophylline indicated
 $\tau = 4 \text{ hr}$ 370



KEUFFEL & ESSER CO., N. Y. NO. 358-110
 Logarithmic, 2 X 2 Cycles.

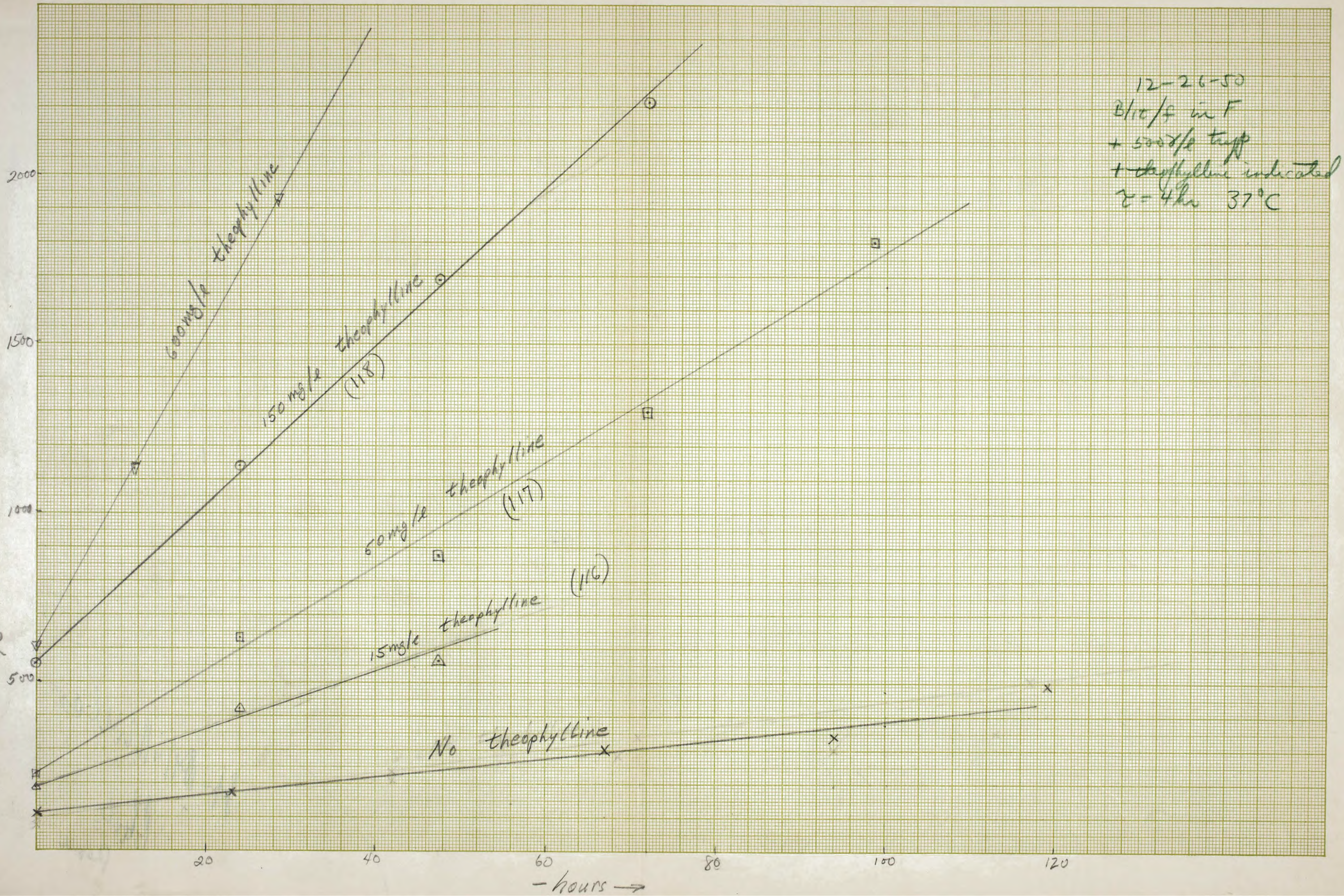
399-14L KEUFFEL & ESSER CO.
Millimeters, 5 mm. lines accented, cm. lines heavy.
MADE IN U.S.A.
Mutation Rate (x100)
(75 RESISTANCE)



12-26-50
B/10/8 mF
+ 500 r/l tupp
+ theophylline (indicated)
 $\tau = 4hr$ 37°C

Concentration Theophylline (mg/l)

388-14L KEUFFEL & ESSER CO.
Millimeters, 5 mm. in diameter
T5-~~REPLACEMENT~~ MUTANTS PER CC



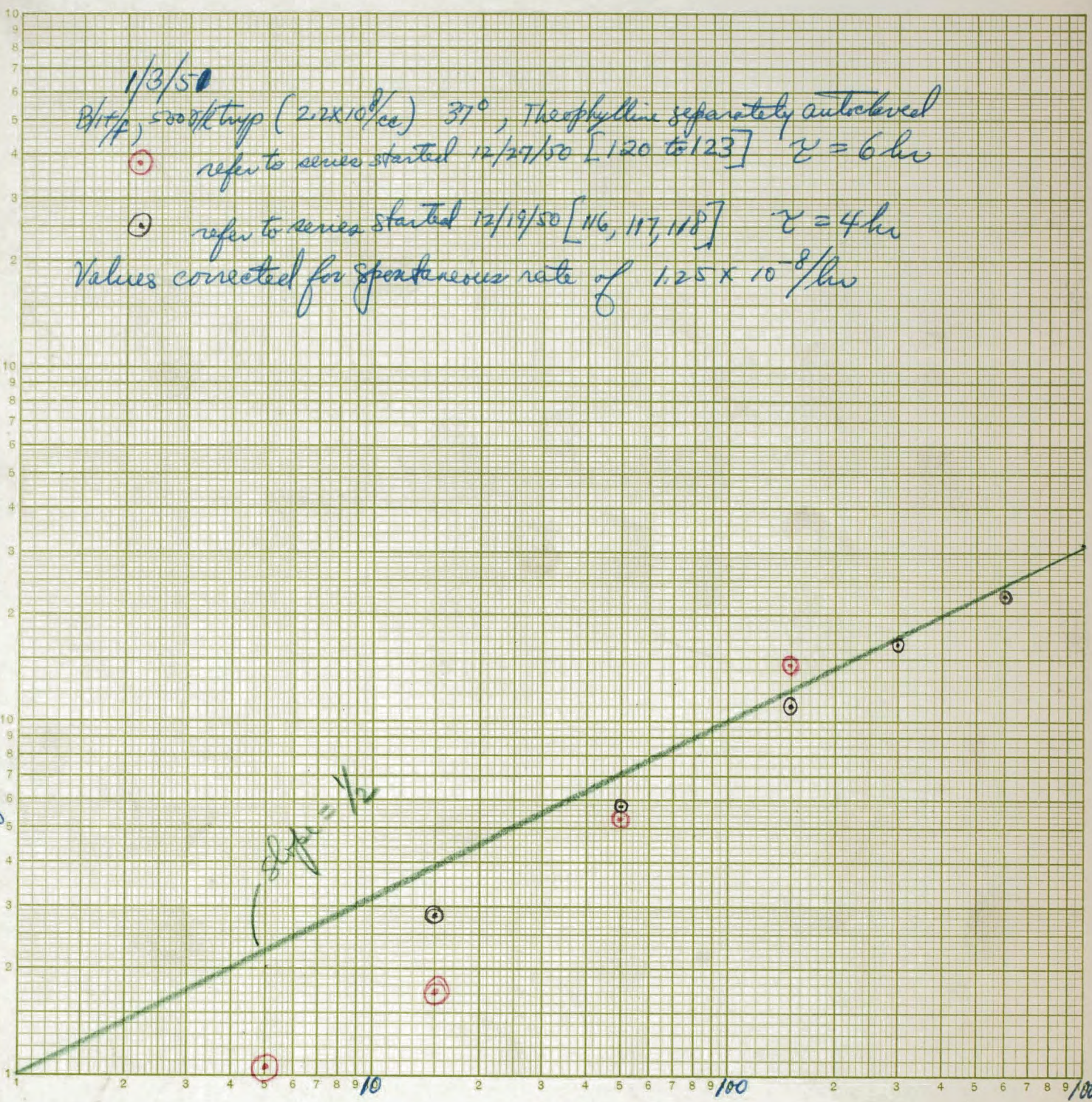
12-26-50
Blc/f in F
+ 5000/l temp
+ theophylline indicated
 $\tau = 4hr$ 37°C

12

H. M. Miller
Chase
Rex

KEUFFEL & ESSER CO. · N. Y. NO. 358-120
 Logarithmic Scale, 10 X 3 Cycles
 Increase mutation rate ($T_5, \times 10^8$)

1/3/50
 8/17/50, 5000/k trip ($2.2 \times 10^8/cc$) 37° , Theophylline separately autoclaved
 refer to series started 12/27/50 [120 to 123] $\tau = 6$ hrs
 refer to series started 12/19/50 [116, 117, 118] $\tau = 4$ hrs
 Values corrected for spontaneous rate of $1.25 \times 10^{-8}/hr$

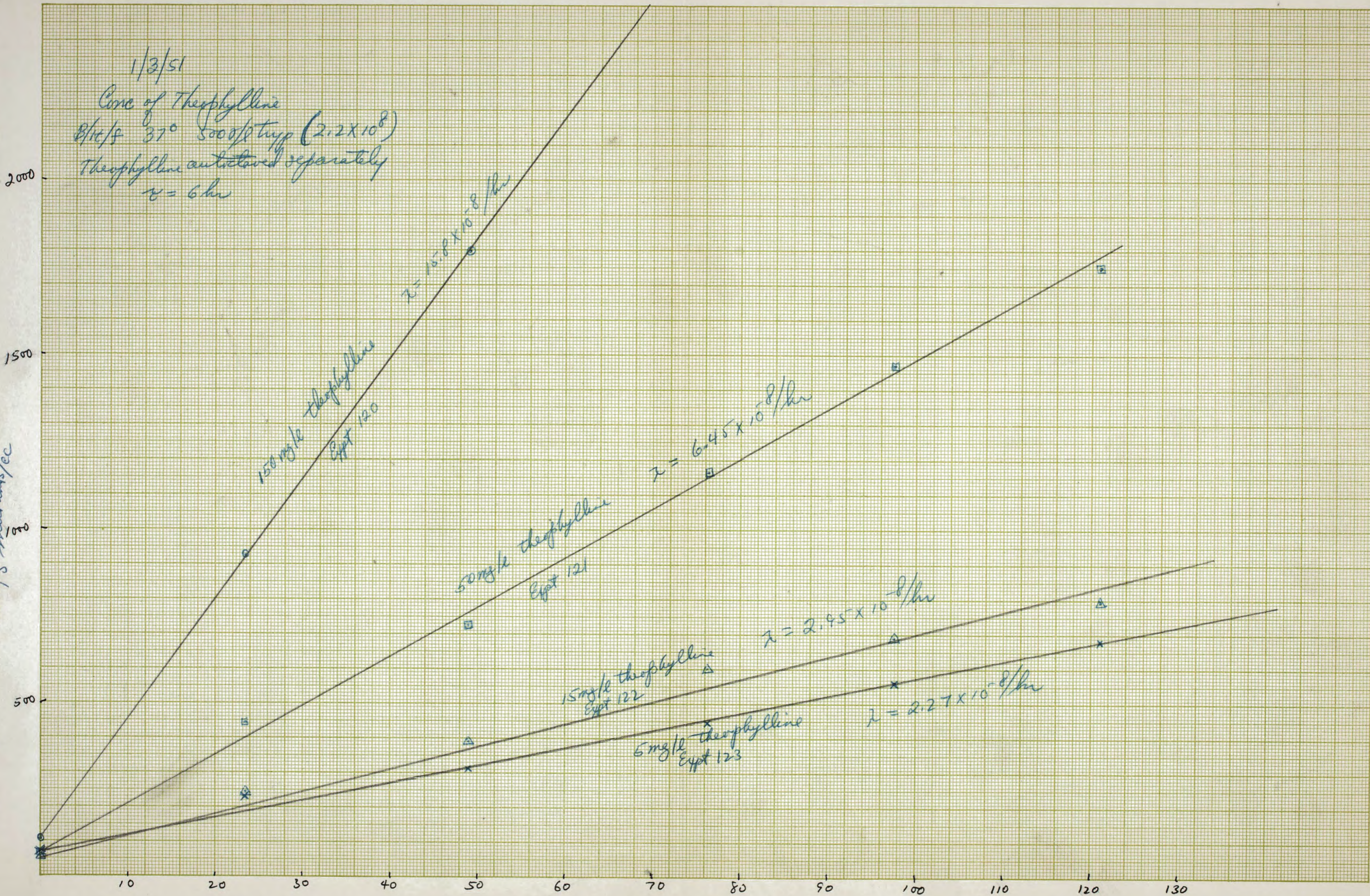


log mg/l Theophylline

1/3/51

Curve of Theophylline
B/c/s 37° 5000/ptupp (2.2×10^8)
Theophylline autotaxed separately
 $\tau = 6 \text{ hr}$

398-141 KEUFFEL & ESSER CO.
Millimeters, 5 mm. lines accented, cm. lines heavy.
MADE IN U.S.A. 75 microns/cc



— hours —>

Series 120 to 123

1/3/51

Conc of theophylline T6 mutants

B/c/s 5000x trip (2.2×10^8 /cc) 37°

$\tau = 6$ hr

T6 mutants

Ratio	T5/T6
150mg/l	11.9
50mg/l	8.2
15mg/l	6.0
5mg/l	5.2

400

300

200

100

T6 mutants/cc

hours

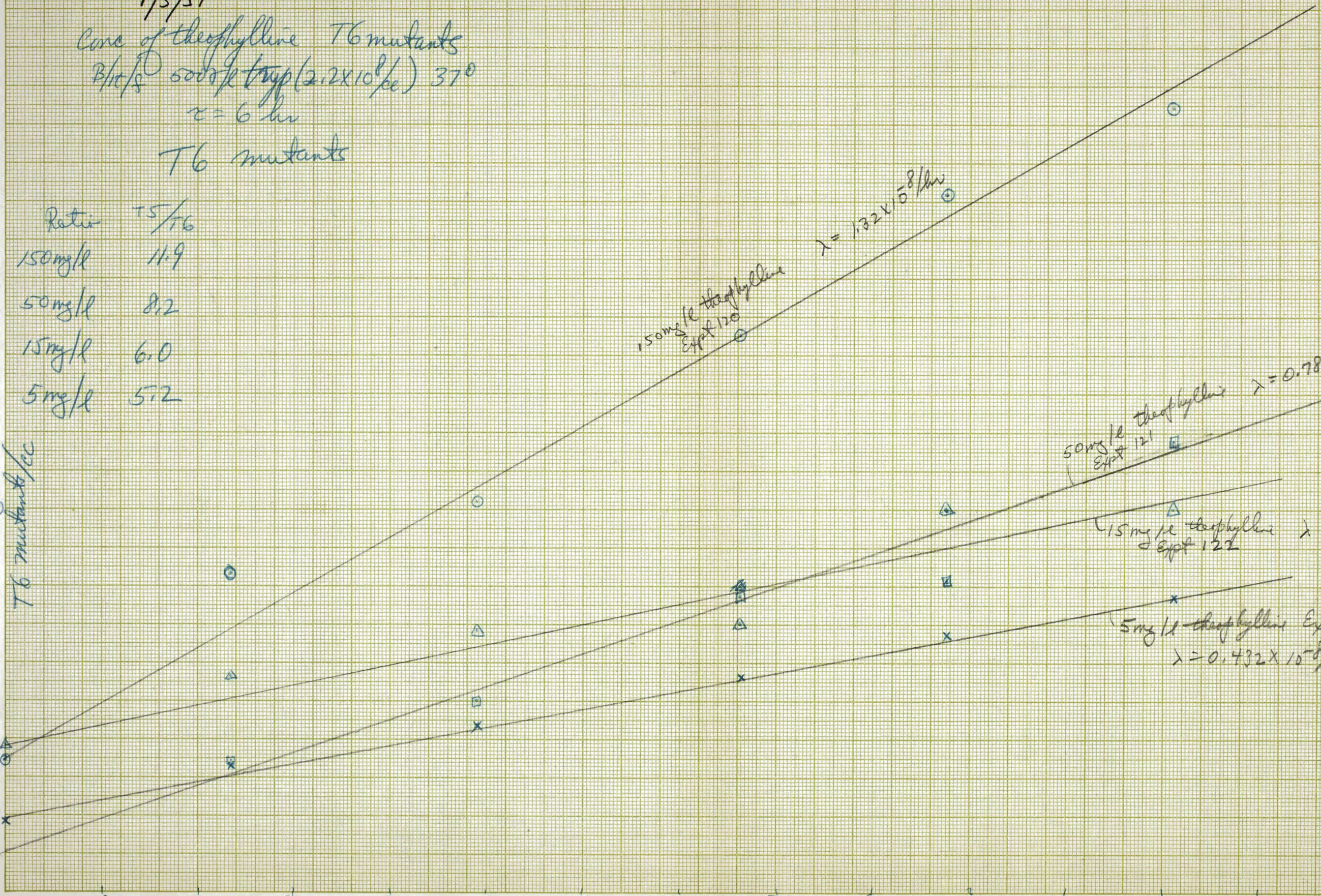
150mg/l theophylline
Expt 120
 $\lambda = 1.82 \times 10^{-8}$ /hr

50mg/l theophylline
Expt 121
 $\lambda = 0.786 \times 10^{-8}$ /hr

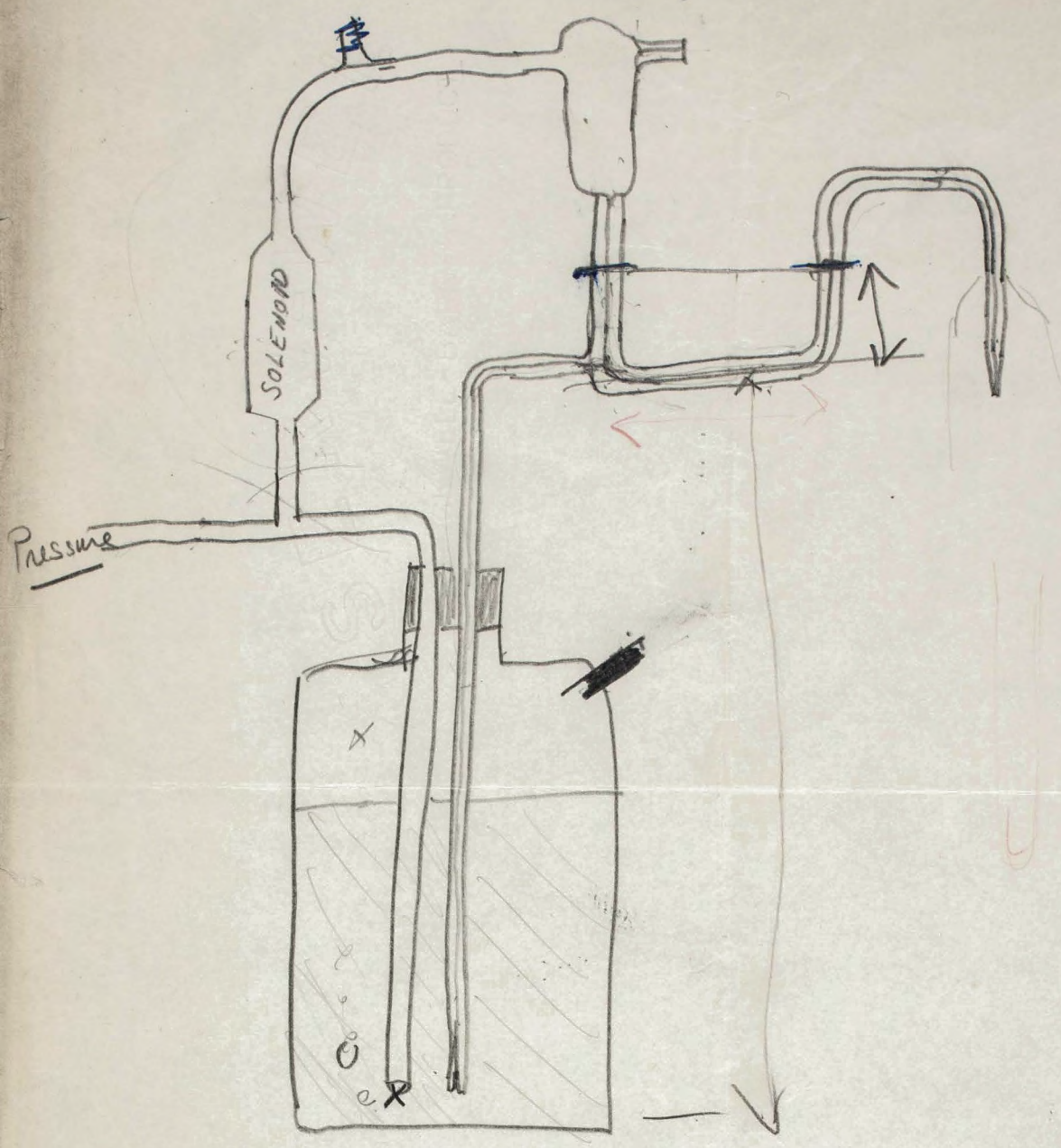
15mg/l theophylline
Expt 122
 $\lambda = 8.49 \times 10^{-8}$ /hr

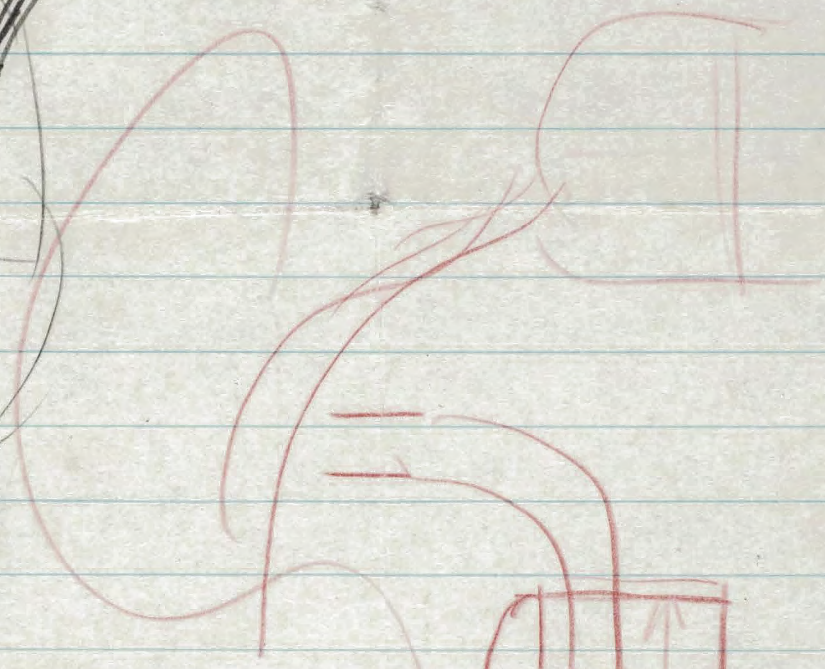
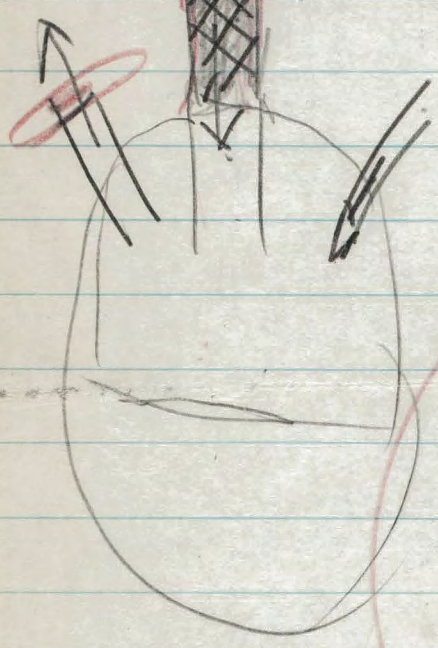
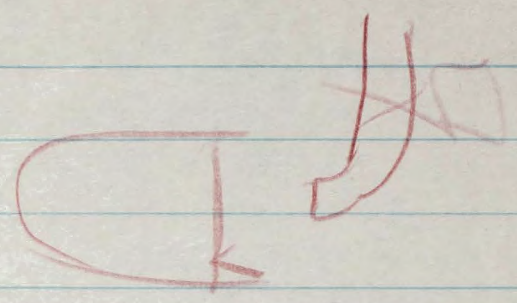
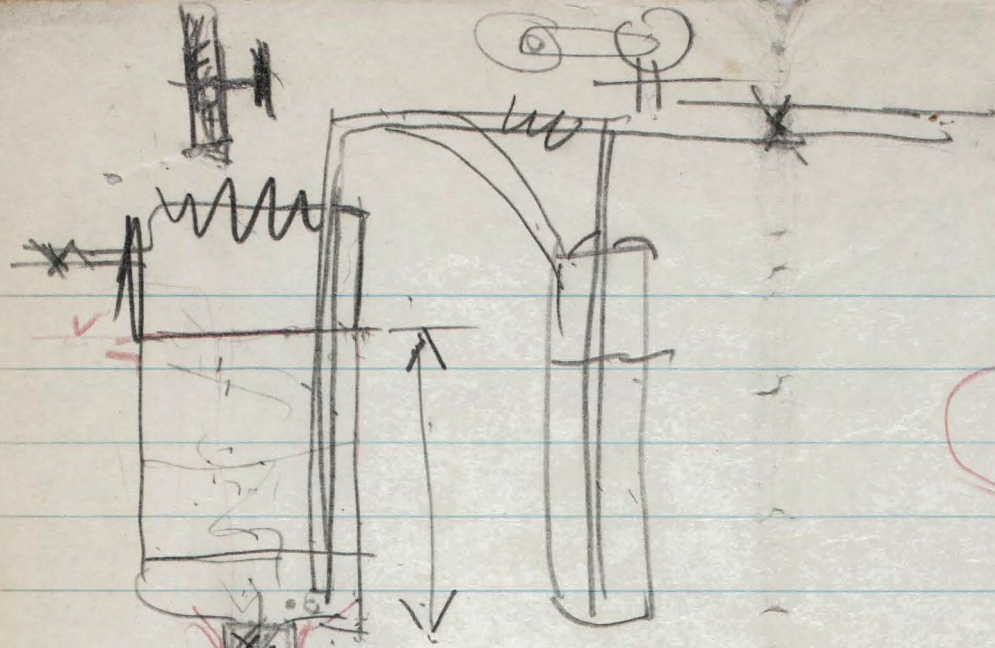
5mg/l theophylline Expt 123
 $\lambda = 0.432 \times 10^{-8}$ /hr

359-141 KEUFFEL & ESSER CO.
Millimeters, 5 mm. Lines accented, cm. lines heavy.
MADE IN U. S. A.



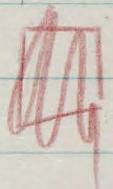
①





~~10/11~~

10/11

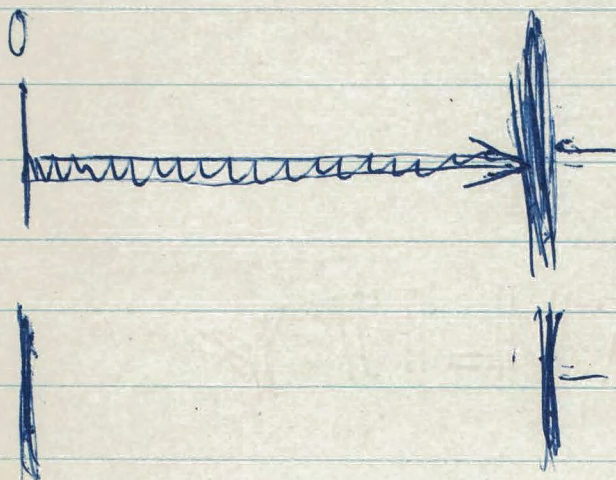


1/5000

23

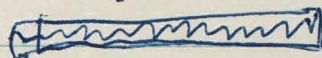
fly

$$\boxed{h = d}$$



flars

10 years



30 kcal / day fly

3000 kg sugar

40 times

$\frac{1}{100}$ kg sugar / kg fly

flar 120

fly

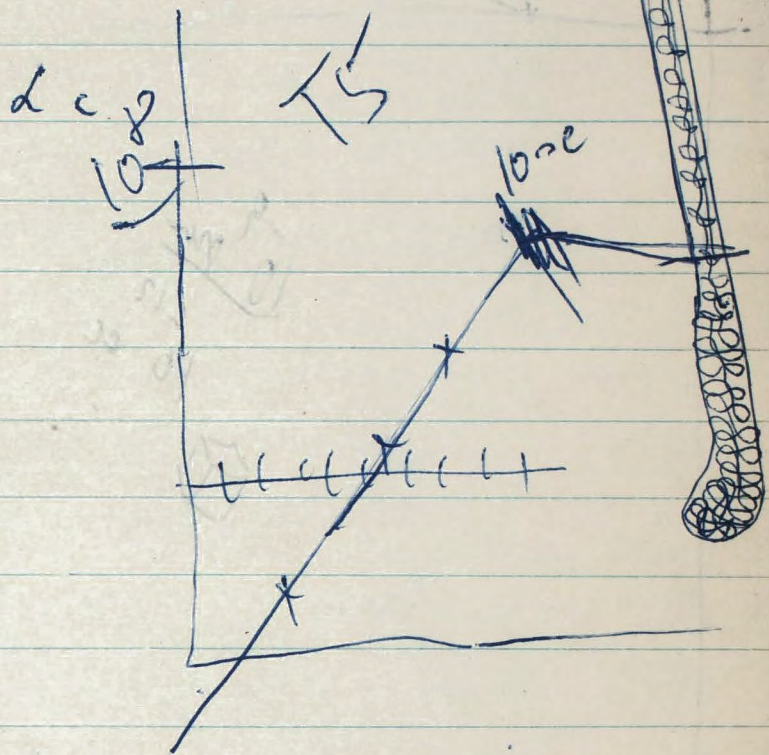
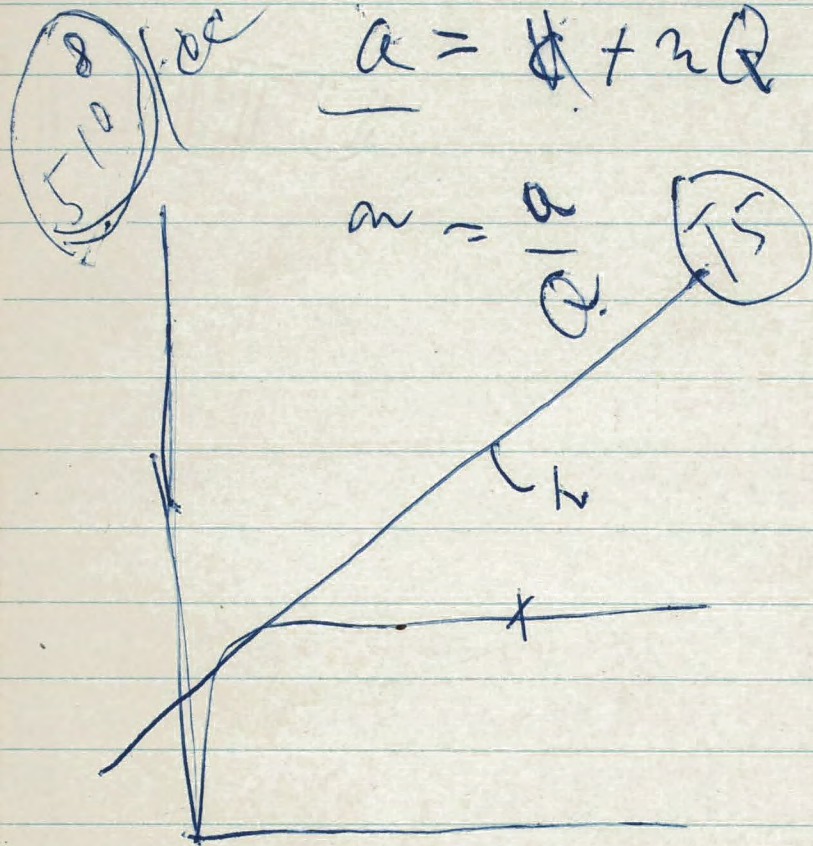
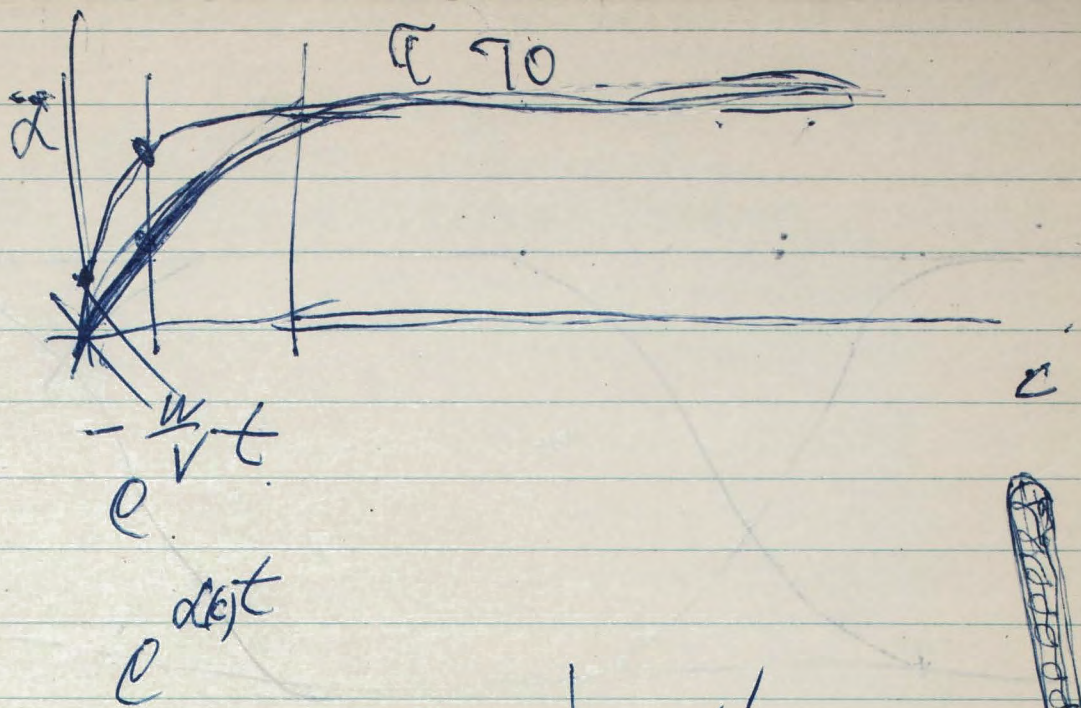
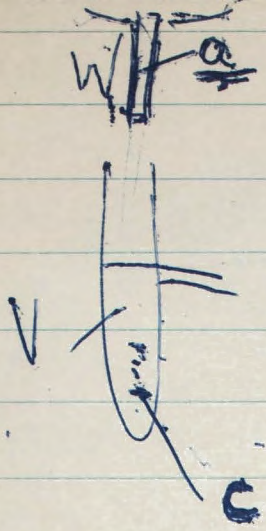
75 kg

$$\boxed{7500}$$

20 ~~min~~ x 7500 min

$$\frac{6000}{4} = 150$$

150 ~~10~~ min = 100



$$i = \frac{w}{RT}$$

$$R = A e^{-3/sec}$$

$$A = 10^{13} / sec$$

$$A = 10^{14} / sec$$

$$A = 10^{15} / sec$$

$$\frac{d f(\lambda, t)}{d t} = c f(\lambda, t)$$

$$\frac{d f(\lambda, t)}{d t} = (\alpha + \beta \lambda) f(\lambda, t)$$

$$(\alpha + \beta \lambda) f(\lambda, t) = c f(\lambda, t)$$

$$(\alpha + \beta \lambda) = c$$

Consider $\int f_n(k) \lambda^k \cdot f_n(c) \lambda^{-k}$
also

This is in the case of

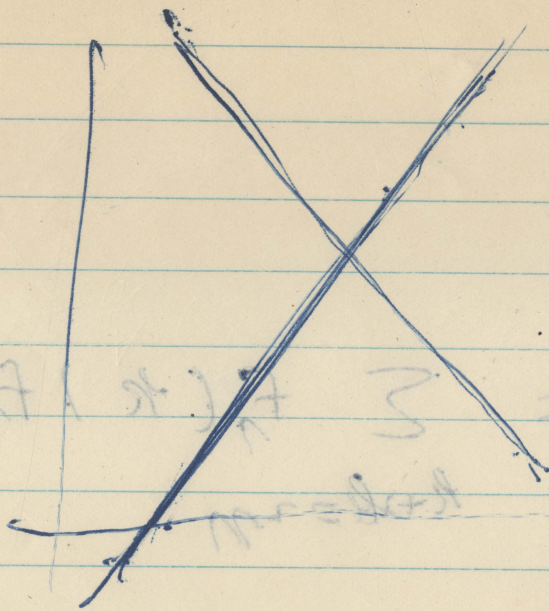
$$g_n(\lambda) g_n(\lambda) = g_n^2(\lambda)$$

$$\frac{df(n)}{dt} =$$

$$f_{n+1}(n) = \sum_{k+l=2n} f_n(k) f_n(l) e^{-\beta 2n}$$

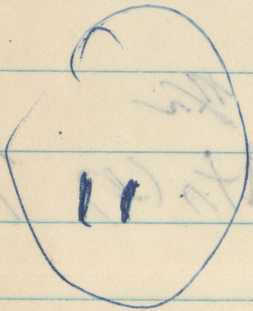
$$\mathcal{F}^m \left[e^{2\beta n} f_{n+1}(n) \right] = \sum_{k+l=2n} f_n(k) \mathcal{F}^m \left[f_n(l) \right]$$

$$\mathcal{F}_{n+1}(\lambda e^{2\beta}) = \mathcal{F}_n^2(\sqrt{\lambda})$$



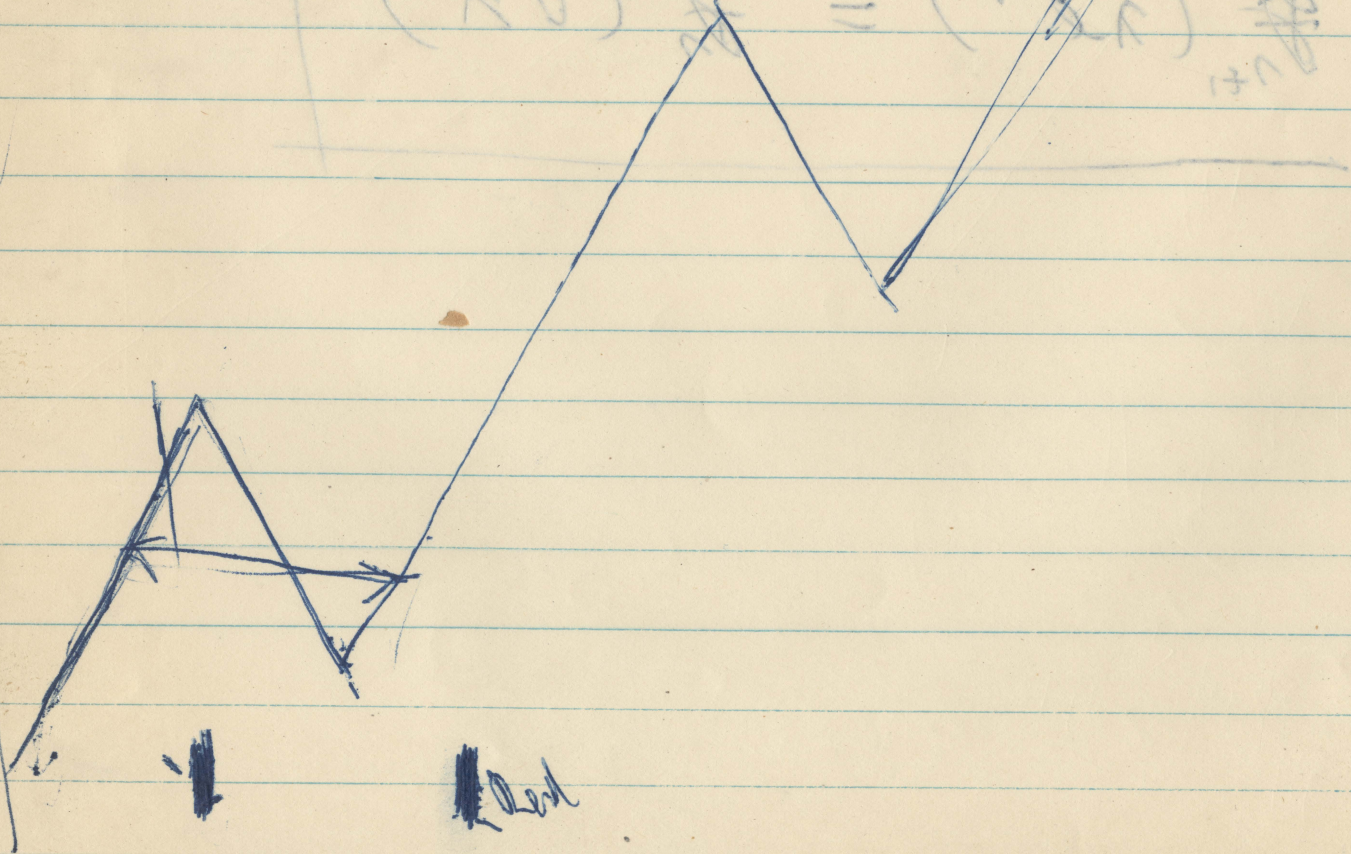
$$= \frac{f(x)}{x}$$

$$f(x) = \sum_{k=1}^n f_k(x) \quad \text{--- beam}$$



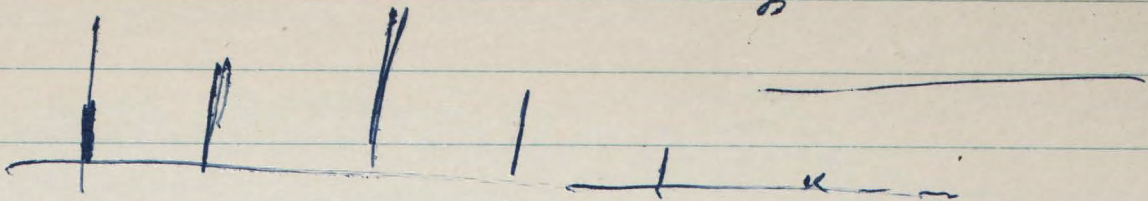
$$f(x) = \sum_{k=1}^n f_k(x) \quad \text{--- beam}$$

$$f(x) = \sum_{k=1}^n f_k(x) \quad \text{--- beam}$$



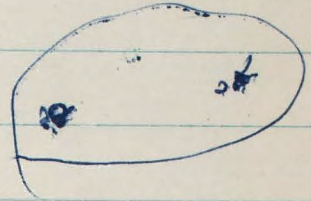
11

11



p_k

$$f(x) = \sum_0^x p_k x^k$$



$$\boxed{f(x)}$$

$$f(f(x)) = \sum_0^x p_k \left(\sum_0^x p_n x^n \right)^k$$

$$g(x)$$

$$f(x) = \sum p_k x^k$$

$$f(x) g(x)$$

$$g(x) = \sum p_k x^k$$

Other assumption: β var.

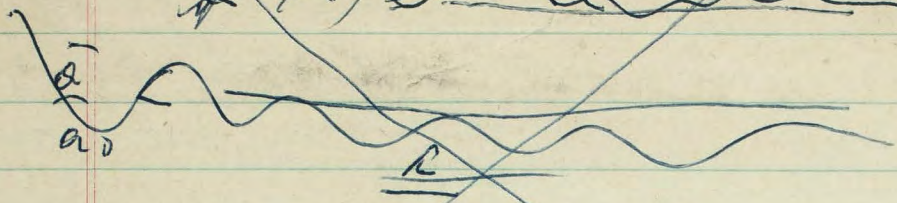
(1)

$$f(n) = \lambda e^{-n\beta} f(n-1)$$

$$f(n) = \frac{\lambda e^{-n\beta}}{\beta} f(n-1)$$

$$\bar{n} = a_0 e^{-n\beta}$$

~~$$f(n) = \frac{\lambda^n}{n!} e^{-\beta n}$$~~



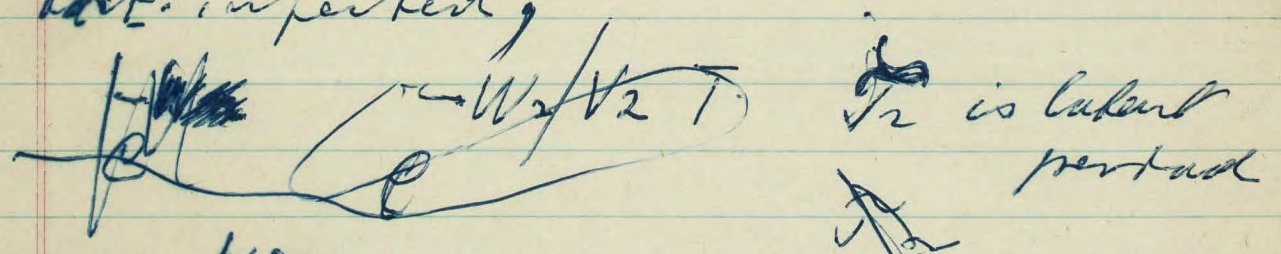
$$f(0), \quad f(0) \lambda e^{-\beta}, \quad f(0) \lambda \left(e^{-\beta} \right)^2 e^{-2\beta}$$

$$\leq \frac{1}{n!} \frac{\lambda^n}{\beta^n} e^{-1+2+3+\dots+n}$$

Prove

Super-Chemostat

Increasing concentration per sec. λ $(n-n)$
 every last. imperfect,



$$e^{-\frac{w_2}{V_2} L}$$

with burst per sec. Given N phage particles

$$\frac{dn}{dt} = \lambda n_0 N e^{-\frac{w_2}{V_2} L(c)} + n_0 \lambda e^{-\frac{w_2}{V_2} L}$$

$$\frac{dn}{dt} = \lambda n_0 N e^{-\frac{w_2}{V_2} L(c)} - n \frac{w_2}{V_2}$$

$$n = \frac{\lambda n_0 N(c) e^{-\frac{w_2}{V_2} L(c)}}{\frac{w_2}{V_2}}$$

Free phage conc.

$$\frac{w_2}{V_2}$$

Free phage ads. neglected

Imperfectness centers n_2

$$\frac{dn_2}{dt} = -n_2 \frac{\omega_2}{V_2} - \frac{n_0 n_0}{V_2} e^{-\frac{\omega_2}{V_2} L(c)} + \frac{n_0 \omega_0}{V_2}$$

$$n_2 = \left\{ 1 - e^{-\frac{\omega_2}{V_2} L(c)} \right\} \frac{n_0 \omega_0}{\omega_2}$$

for large V_2 small $\omega_2 L(c)$ $n_2 \approx \frac{n_0 \omega_0}{\omega_2}$

in coming from atmosphere $\omega_0, n_0, \omega_0 \in$

incoming from side branch, $\omega_2 \sim \omega_0$, $(\omega_2 - \omega_0) a_2$,

Thyristor balance thyristor balance a_2

$$(\omega_2 - \omega_0) a_2 + \omega_0 c_0 = \frac{1}{2} \tau(c_0) n_2 V_2 + \dots$$

$$\frac{1}{2} \tau(c_0) n_0 \omega_0 V_2 + \omega_2 c_2$$

$$\frac{(\omega_2 - \omega_0) a_2 + \omega_0 c_0}{\omega_2} = \frac{1}{2} \tau(c_0) \frac{n_0 \omega_0 V_2}{\omega_2} + c_2$$

is c enough for full phase output

$$c = 10^{-9} \text{ gm} \quad \text{barrier} \quad 2 \cdot 10^{-15}$$

$$5 \cdot 10^8 \times 2 \cdot 10^{-15} = 10^{-6} \text{ gm/cm}^2$$

gm/gm/sec
gm/vol
(Vol) sec
gm

if phase 1% of thyristor balance it takes 10 times c for full yield

interesting case: slow flow $\frac{1}{V} \omega_2 \gg L$
and looks for mutant/mild type

Imperfectly centered m_2

(3)

$$(1) \quad m_2 = \frac{m_0 \omega_0}{\omega_2} \left(1 - e^{-\frac{\omega_2}{V_2} L(c_2)} \right)$$

Pythagorean balance

gm/sec

~~cm/sec~~

$$(2) \quad (\omega_2 - \omega_0) a_2 + \omega_0 c_0 = f(c_2) m_2 V_2 + \omega_2 c_2$$

~~from (1) $m_2 = \frac{m_0 \omega_0}{\omega_2} \left(1 - e^{-\frac{\omega_2}{V_2} L(c_2)} \right)$~~

$$\text{from (2) } (\omega_2 - \omega_0) a_2 + \omega_0 c_0 = f(c_2) \frac{m_0 \omega_0}{\omega_2} \left(1 - e^{-\frac{\omega_2}{V_2} L(c_2)} \right) + \omega_2 c_2$$

~~Labels should be at dirn of c_2~~

~~for gm/sec $[c_2]$ to ω_2~~

from (1) $m_2 \approx \frac{m_0 \omega_0}{V_2} L(c_2)$

and (2) preserved:

gm/sec

$$(\omega_2 - \omega_0) a_2 + \omega_0 c_0 \approx f(c_2) m_0 \omega_0 L(c_2) + \omega_2 c_2$$

$$(\omega_2 - \omega_0) a_2 + \omega_0 c_0 \approx f_0 c_0 m_0 \omega_0 + \omega_2 c_2$$

$$(3) \quad c_2 \approx \frac{\omega_2 - \omega_0}{\omega_2} a_2 + \frac{\omega_0}{\omega_2} c_0 = f_0 c_0 m_0 \frac{\omega_0}{\omega_2}$$

better $\downarrow \downarrow$ ~~same~~ $\downarrow \downarrow$

if H is taken up per phase and phase yield is constant M

and if V_2 very large

$a(\omega_2 - \omega_0) + c_0 \omega_0$ is coming in; $AM m_0 \omega_0$ is taken up; $c_2 \omega_2$ is leaving

$$a(\omega_2 - \omega_0) + c_0 \omega_0 = AM m_0 \omega_0 + \omega_2 c_2$$

for large V_2 so that no imperfect centers are washed out

What is wrong with the
 like differential equation?

$$(1) \frac{df(t)}{dt} = +k_1 f(t-1) + \bar{a}_0 f(t) - k_1 f(t) - \beta f(t)$$

$$(2) \frac{df(t)}{dt} = \bar{a} f(t)$$

$$\bar{a} f(t) = k_1 f(t-1) + a_0 e^{-\beta t} f(t) - k_1 f(t)$$

$$f(t) (\bar{a} + k_1 - a_0 e^{-\beta t}) = k_1 f(t-1)$$

$$(3) f(t) = \frac{k_1 \times f(t-1)}{\frac{\bar{a}}{a_0} + \frac{k_1}{a_0} - e^{-\beta t}}$$

$$\underline{a_0 = 1}$$

$$f(t) = \frac{k_1 f(t-1)}{\bar{a} + k_1 - e^{-\beta t}}$$

$$\bar{a} + k_1 > e^{-\beta}$$

$$\frac{df(0)}{dt} = \bar{a}_0 f(0) - k_1 f(0)$$

$$\bar{a} f(0) = a_0 f(0) - k_1 f(0)$$

$$\frac{\bar{a}}{a_0} = 1 - \frac{k_1}{a_0} \quad (4) f(t) = \frac{k_1 f(t-1)}{1 - e^{-\beta t}}$$

$$\frac{\bar{a}}{a_0} + \frac{k_1}{a_0} = 1$$

2nd problem

(2)

$$\frac{df(n)}{dt} = \beta f(n-1) + \lambda_2 f(n-2) + a_0 f(n) - (\lambda_1 + \lambda_2) f(n)$$

$$\frac{df(n)}{dt} = \bar{a} f(n)$$

$$\left(\bar{a} + \lambda_1 + \lambda_2 \right) f(n) e^{-\beta n} = \lambda_1 f(n-1) + \lambda_2 f(n-2)$$

$\lambda_0 = 1$

$$f(n) = \frac{\lambda_1 f(n-1) + \lambda_2 f(n-2)}{\bar{a} + \lambda_1 + \lambda_2 - e^{-\beta n}}$$

$$f(n) = (\lambda_1 + \lambda_2)^n$$

$$f(n) = \frac{\lambda_1 (\lambda_1 + \lambda_2)^{n-1} + \lambda_2 (\lambda_1 + \lambda_2)^{n-2}}{\lambda_1 + \lambda_2}$$

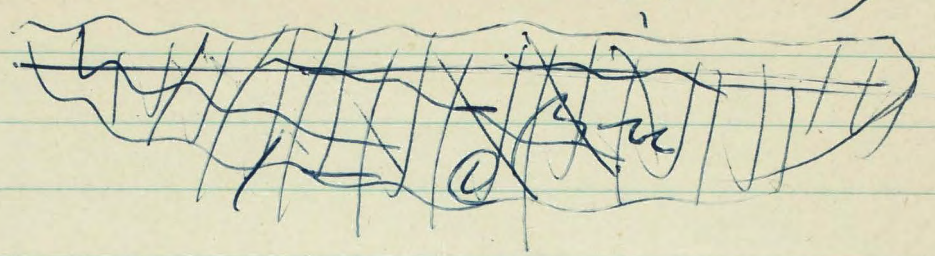
$$\frac{df(0)}{dt} = a_0 f(0) - (\lambda_1 + \lambda_2) f(0)$$

$$\bar{a} f(0) = a_0 - \lambda_1 - \lambda_2$$

$$\frac{\bar{a}}{a_0} = 1 - \frac{\lambda_1}{a_0} - \frac{\lambda_2}{a_0}$$

$$f(n) = \frac{\lambda_1 (\lambda_1 + \lambda_2)^{n-2} (\lambda_1 + \lambda_2) + \lambda_2 (\lambda_1 + \lambda_2)^{n-2} (\lambda_1)^2 (\lambda_1 + \lambda_2) + \lambda_1 \lambda_2 (\lambda_1 + \lambda_2)^{n-2} + \lambda_2 (\lambda_1 + \lambda_2)^{n-2}}{\lambda_1 + \lambda_2}$$

$$f(n) = \underline{\lambda_1} f(n-1) + \underline{\lambda_2} f(n-2) + \dots + \lambda_k (n-k)$$



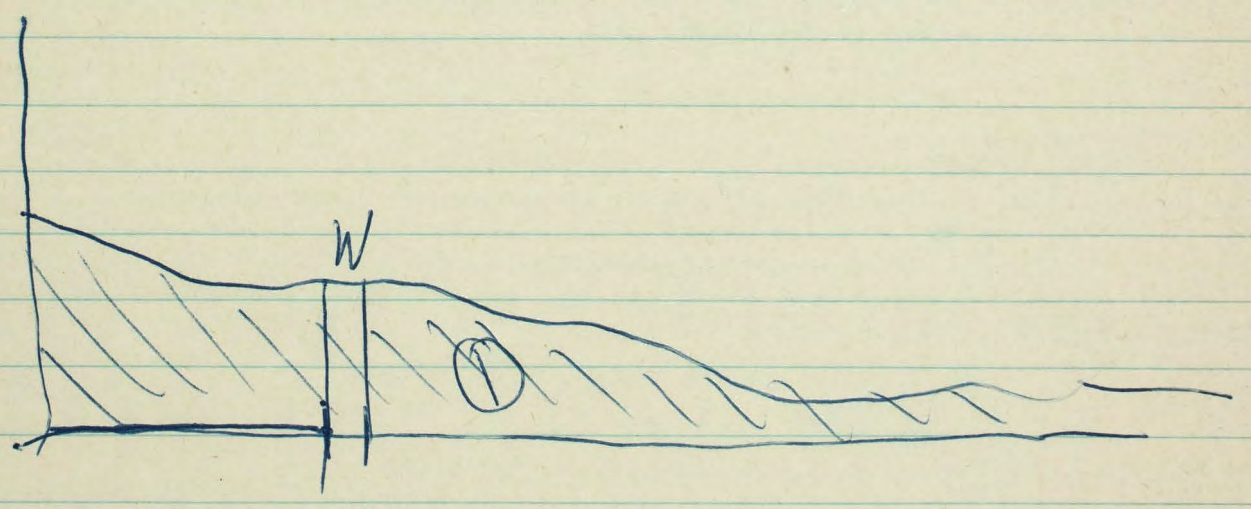
$$f(n) = k f(n-1)$$

$$f(n) = \frac{A(n)}{B(n)}$$

$$k f(n-2) = \lambda_1 k f(n-2) + \lambda_2 f(n-2)$$

$$k^2 = \lambda_1 k + \lambda_2$$

$$k = \underline{\lambda_1 + \lambda_2}$$



Typographium absorption

(4)

assume 10 \AA square area $\approx 10^{-14} \text{ cm}^2$
 each molecule ~~has~~ $\frac{10^5 \times 10^{-14}}{6 \cdot 10^{23}} = \frac{1}{6} 10^{-18} \text{ gm}$

~~1000~~ of molecules ~~has~~ $\frac{10^{-12} \times 10^{-3}}{\frac{1}{6} 10^{-18}} =$

~~6000 x 10¹⁴ = 6 x 10¹⁷ cm² area~~

~~6000~~ $6 \cdot 10^6$ molecules $\times 10^{-14} \text{ cm}^2$
 $6 \times 10^6 \cdot 10^{-14} = 6 \cdot 10^{-8} \text{ cm}^2$

$$10^{13} \left(e^{-\frac{2}{RT}} \right) \left(\frac{1}{a} \right)^{30} \approx (1000)$$

$$60 \times \frac{1}{a} \times 2 \cdot 10^4 \left(\frac{1}{a} \right)^{30} = 1000$$

60x

Terphenol ~~is~~ dissolved in Styrene
 5% Hopfinger Toluene

Ka₂ (Horslow) for f rays

Fisch (Grand Central)

Fisch - Besouls full of France (no measurement) after that: measurement in May Birmingham
 & not in Liverpool - Peters -
 Petrows - Brown

Wesley Park II

(1)

$$f(n) = \frac{\lambda}{\lambda - \lambda_0 e^{-\beta n}} f(n-1)$$

$$\{n-1 \geq 0\}$$

$$[\lambda > \lambda_0 e^{-\beta}]$$

$$f(n) > \frac{\lambda/\lambda_0}{1 - e^{-\beta n}} f(n-1)$$

for small βn (also true for large βn)

$$f(n) \approx \frac{\lambda/\lambda_0}{\beta n} f(n-1) \quad (\beta n > 1 - e^{-\beta n})$$

$$\frac{\lambda}{\lambda_0} < \frac{f(0) + f(1)e^{-\beta} + f(2)e^{-2\beta}}{f(0) + f(1) + f(2) + \dots}$$

$$f(1) = \frac{\lambda/\lambda_0}{\beta} f(0)$$

$$f(2) = \frac{(\lambda/\lambda_0)^2}{2(\beta)^2} f(0)$$

$$f(3) = \frac{(\lambda/\lambda_0)^3}{3(\beta)^3} f(0)$$

$$\frac{f(n)}{f(0)} = \frac{(\lambda/\lambda_0)^n}{n! (\beta)^n}$$

$$\frac{\lambda}{\lambda_0} < \frac{\sum_0^{\infty} \frac{1}{n!} \left(\frac{\lambda/\lambda_0}{\beta}\right)^n}{e^{\lambda/\lambda_0 \cdot e^{-\beta}}} = e^{\lambda/\lambda_0 \cdot e^{-\beta}}$$

~~$\frac{\lambda}{\lambda_0} < \frac{\lambda}{\lambda_0 \beta (1-\beta)}$~~

~~$e^{-\lambda/\lambda_0} > e^{-\beta}$~~

~~$\frac{\lambda}{\lambda_0} < \beta$~~

Mon 22 30 W E 1 day

(2)

30 WE 1 day kg \approx 1.2 kg 9 hours

Mon or per hour and kg $\frac{1.2}{9} = \frac{1}{7.5}$ W/A

acteria 4000 WE / kg hour

factor Mon to bacteria about 3500
or $\frac{1}{10}$ of a day in bacteria = 1 year in

Mon - 2.4 hours or $\approx \frac{1}{2}$ d.

Repeat from scratch

Population $N = f(0) + f(1) + f(2) + \dots + f(n) + \dots$

$$\bar{a} = \frac{1}{N} \frac{dN}{dt} \quad \text{or} \quad \frac{dN}{dt} = \bar{a} N \quad (1)$$

In the substrate

growth rate of bacteria containing n mutations $\alpha(n) = \alpha_0 e^{-\beta n} \quad (2)$

Steady state: $\frac{df(n)}{dt} = \bar{a} f(n) \quad (3)$

But $\frac{df(n)}{dt} = \alpha f(n-1) + \frac{1}{2} \alpha_0 e^{-\beta n} f(n) \quad (4)$

from (3) and (4) we obtain

$$\bar{a} f(n) = \alpha_0 e^{-\beta n} f(n) + \alpha f(n-1)$$

$$f(n) = \frac{\alpha f(n-1)}{\bar{a} - \alpha_0 e^{-\beta n}} = \frac{\alpha \alpha_0^n f(n-1)}{\bar{a} - \alpha_0 e^{-\beta n}} \quad (5)$$

since f must be positive and finite for all $n \geq 1$

$$\bar{a} > \alpha_0 e^{-\beta} ; \quad \frac{\bar{a}}{\alpha_0} > e^{-\beta} \quad (6)$$

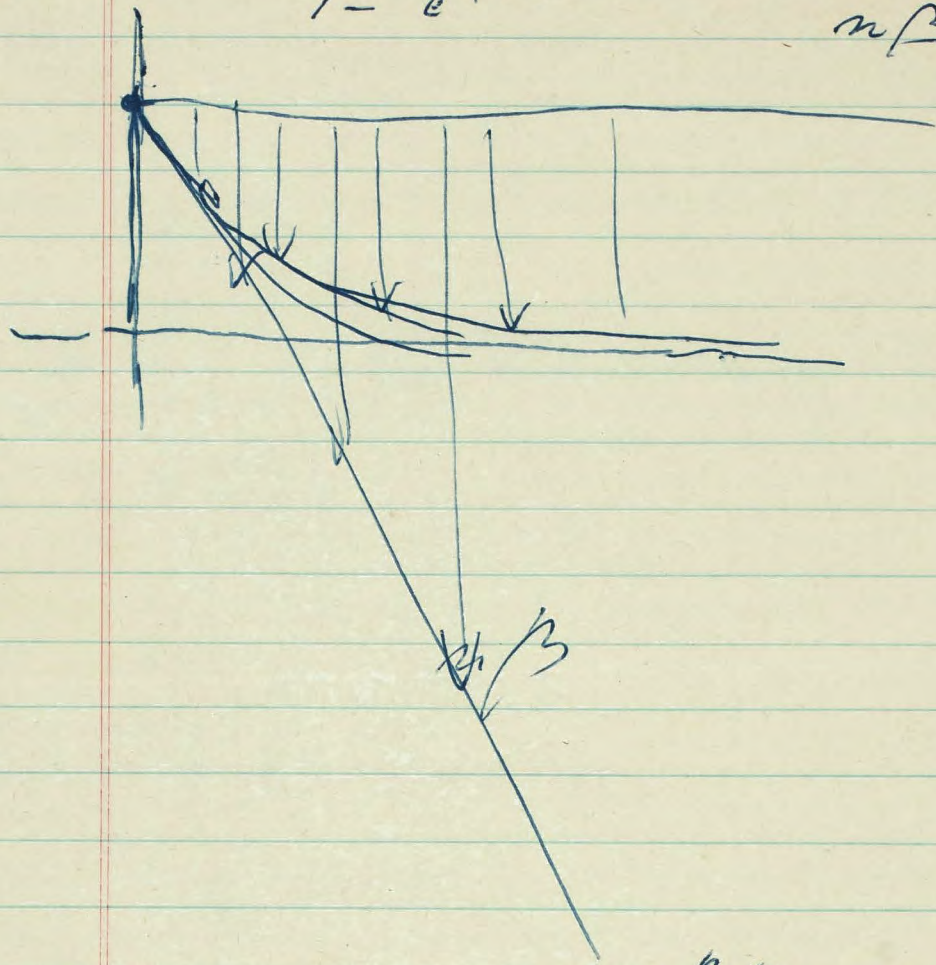
~~(*)~~

From (5) we obtain since $\frac{\alpha}{\lambda_0} < 1$

$$f(n) > \frac{\lambda/\lambda_0 f(n-1)}{1 - e^{-\beta n}}$$

and we further obtain, since $n\beta > 1 - e^{-\beta n}$

$$(7) \quad f(n) > \frac{\lambda/\lambda_0 f(n-1)}{1 - e^{-\beta n}} > \frac{\lambda/\lambda_0 \times f(n-1)}{n\beta} = f^*(n)$$



$f(n) = f^*(n) + A(n)$
where $A(n) > 0$

$$(8) \quad \bar{x} = \frac{\lambda_0 (f(0) + f(1)e^{-\beta} + f(2)e^{-2\beta} + \dots + f(n)e^{-\beta n})}{f(0) + f(1) + f(2) + \dots + f(n)}$$

Now if $f^* \in L$

~~$a = \frac{A+B}{A+B}$~~
 ~~$a = \frac{\text{const.} + A}{\text{const.} + A}$~~

Now if $f^* \in L$ so that

$$f(n) = f^*(n) + A(n) \text{ (proven)}$$

from (8)

$$\frac{\bar{x}}{\lambda_0} = \frac{f(0) + f(1)e^{-\beta} + \dots + (f^*(n) + A(n))e^{-\beta n} + \dots}{f(0) + f(1) + \dots + f^*(n) + A(n) + \dots}$$

We can now show that

$$\frac{\bar{x}}{L_0} \leq \frac{f(0) + f(1)e^{-\beta} + f(2)e^{-2\beta} + \dots + f(n)e^{-n\beta} + \dots}{f(0) + f(1) + f(2) + \dots + f(n) + \dots} \quad (4)$$

In order to show that we write

$$(9) \frac{\bar{x}}{L_0} = \frac{A(n) + \cancel{A(n)} + \Delta(n)e^{-n\beta}}{B(n) + \cancel{A(n)} + \Delta(n)} < \frac{A(n)}{B(n)}$$

and have then to show that

$$\frac{A(n)}{B(n)} - \frac{A(n) + \Delta(n)e^{-n\beta}}{B(n) + \Delta(n)} \geq 0$$

$$\text{or } \cancel{A} + A + \Delta(n) - \cancel{A} - B\Delta(n)e^{-n\beta} > 0$$

$$(10) \quad A(n) - B(n)e^{-n\beta} > 0$$

In order to see that we write

$$\text{for (6)} \quad \frac{\bar{x}}{L_0} > e^{-\beta} \quad \text{from (9)}$$

$$\frac{A(n) + \Delta(n)e^{-n\beta}}{B(n) + \Delta(n)} > e^{-\beta}$$

$$(11) \quad \text{or } A + \Delta(n)e^{-n\beta} - B(n)e^{-\beta} - \Delta(n)e^{-\beta} > 0$$

$$\text{or } \cancel{A} - B(n)e^{-\beta} > \Delta(n)e^{-\beta} - \Delta(n)e^{-n\beta}$$

$$\text{or } A - B(n)e^{-\beta} > 0$$

$$\text{or } A > B(n)e^{-\beta}$$

$$\text{but since } B(n)e^{-\beta} > B(n)e^{-n\beta}$$

$$\text{we have } A > B(n)e^{-n\beta}$$

which is identical with (10)

We may therefore write

$$\frac{\bar{x}}{L_0} \leq \frac{f(0) + f(1)e^{-\beta} + f(2)e^{-2\beta} + \dots + f(n)e^{-n\beta} + \dots}{f(0) + f(1) + f(2) + \dots + f(n) + \dots}$$

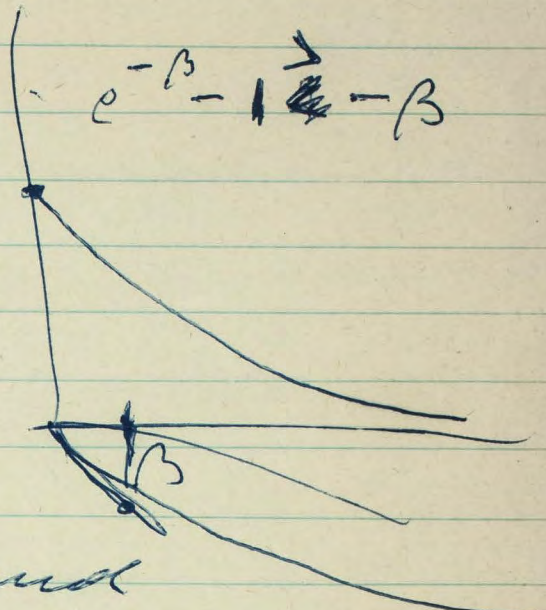
(5)

and from (7)

$$\frac{\bar{d}}{d_0} \leq \frac{1 + \frac{\lambda/d_0}{\beta} e^{-\beta} + \frac{(\lambda/d_0)^2}{1.2\beta^2} e^{-2\beta} + \dots + \frac{(\lambda/d_0)^n}{n! \beta^n} e^{-n\beta}}{1 + \frac{\lambda/d_0}{\beta} + \frac{\lambda/d_0}{1.2\beta^2} + \dots + \frac{(\lambda/d_0)^n}{n! \beta^n}}$$

$$= \frac{e^{\frac{\lambda/d_0}{\beta}} e^{-\beta}}{e^{\frac{\lambda/d_0}{\beta}} [e^{-\beta} - 1]} = e^{\frac{\lambda/d_0}{\beta}} [e^{-\beta} - 1]$$

$$= e^{\frac{\lambda/d_0}{\beta}} \times [e^{-\beta} - 1]$$



or for small β

(12) $\frac{\bar{d}}{d_0} \leq e^{-\frac{\lambda}{d_0}}$

But on the other hand

from (6) $\frac{\bar{d}}{d_0} > e^{-\beta}$

Thus from (6) and (12)

$$e^{-\beta} \leq e^{-\frac{\lambda}{d_0}}$$

or $\frac{\lambda}{d_0} < \beta$

(13)

~~~~~

for any  $\beta$  we must have from (5) for large  $n$  and  $m$

$$f(m) = \left(\frac{\lambda}{d_0}\right)^{m-n} f(n)$$

so it must be  $\frac{\lambda}{d_0} < 1$

(14) or  $\lambda < \bar{d} < d_0$   
or  $\frac{\lambda}{d_0} < 1$