

On Nuclear Chain Reactions and their Bearing on the Question
of Power Production.

Sir,

I wish to draw attention to ~~the~~ theoretically possible transmutation processes of a special type and indicate simple experiments which could lead to their detection. The energy liberated in a process of this type may very well be large as compared to the energy input required for the maintenance of the process; if such a process can be realised and is used for the generation of power we may therefore have an active power balance. For instance by radiating a metastable element with neutrons it may prove to be possible to maintain a process in which neutrons cause a metastable element to transmute without being stopped from further remaining active in the process and increasing their average energy and number i.e. we may have a nuclear chain reaction. It is believed

28th July, 1934.

Memorandum of Possible Industrial Applications arising
out of a New Branch of Physics.

It is possible to indicate methods which might be successfully applied for the purpose of liberating atomic energy. It is not possible to foretell with certainty that these methods will be successful, but the experiments necessary for ascertaining this are fairly simple and could be carried out on a small scale in the university laboratories. Should such experiments give favourable results, the production of energy and its use for power production would be possible on such a large scale and probably with so little cost that a sort of industrial revolution could be expected; it appears doubtful, for instance, whether coal mining or oil production could survive after a couple of years.

I have applied for a group of patents in order to obtain patent protection for those methods which seemed to me promising, and it appears that these patents were successful in foreshadowing the latest developments in physics.

They include, for instance, methods for the artificial production of radio-active bodies based on a process which recently has been discovered by Fermi. The production of artificial "radium" for medical purposes based on these processes seems to be a sound commercial proposition, but it would be sidetracking the issue to concentrate on this point.

Facilities are required for two different purposes:-

1.) In order to develop and maintain a group of valid patents £500 are required for the next year, which would also take care of administrative expenses connected with the maintenance of the patents.

2.) If we wish to start the necessary experiments one ought to secure the continuity of work for two to three years. It is not possible to state exactly what facilities will be required as this will depend to a large extent on what facilities will be provided by the university laboratory which would be used as a frame for this work. It would, however, be advisable to have £2,000 available for expenditure that may be incurred.

From the point of view of a financier who could consider contributing to the required facilities the position is this:- the chances that the envisaged experiments will yield a favourable result may be estimated to anything between 1 to 20 and 1 to 5. The value of the return in case of success is, of course, enormous and could hardly be estimated in terms of money, so that from the purely financial point of view it is a sort of lottery with a fairly good chance to win a prize and enormous prizes. Yet it would be highly preferable to get financial support from quarters that would consider the experiments as a research work in the field of science which has a good chance of highly significant industrial applications, and realise that the exploitation of discoveries of this scope must not be organised on a purely commercial basis.

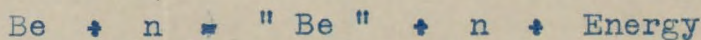
But Difficulty will undoubtedly arise from the fact that it is not easy for anybody to form an independent opinion of his own on the merits of the case. A possible way out would be, to get the opinion of some of the professors of the University of London who are working themselves in this field, and with whom I can easily keep in touch on the matter.

Suggested Experiments for the Detection of
Nuclear Chain Reactions, and the Liberation
of Nuclear Energy.

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I wish to draw attention to theoretically possible transmutation processes of a special type and indicate simple experiments which could lead to their detection. The energy liberated by them ~~may very well~~ ^{would} be large as compared to the energy input ~~that~~ ^{which} is required for the maintenance of the process.

The simplest type may be obtained by radiating a metastable element with neutrons. Some elements betray their metastable character by being radio-active; others are not radio-active. The mass of Beryllium seems to be sufficient to allow a spontaneous transmutation (for instance into two alpha particles and a neutron) which apparently is inhibited. Such inhibition ~~may~~ ^{might} however, be lifted in a nuclear collision with a neutron; a neutron hitting a Beryllium nucleus would then liberate energy without getting captured and could go on hitting efficiently further Beryllium nuclei, the total number of its efficient collisions, and the total amount of the liberated energy being limited by the geometrical conditions only. We shall call a reaction of this type a "chain".



"Be" would be an isomer of Be, which would or would not break up into parts.

Additional neutrons could be liberated along some such chains, which will then be called "divergent" in this note.

A metastable element must necessarily be involved in a chain in which only one kind of non-positive nucleus, as the neutron, n^1 , forms the links of the chain. (~~singulet~~ chain).

It is theoretically possible to maintain chains in mixtures of stable elements and also in certain pure stable elements if two different kinds of non-positive nuclei form the links of the chain (~~or other particles~~). The *detailed* discussion of such chains had better be postponed, pending conclusive evidence which would show that neutrons of the mass number two or negative protons (or other particles which could, together with the neutron, serve as links in such chains) have been actually generated in the laboratory.

Divergent Chains in Stationary Processes.

Some information on the geometrical conditions in which a stationary process can be maintained and on the order of magnitudes involved can be obtained by considering a closed spherical layer in which a divergent chain is maintained by a neutron source placed in the centre of the hollow sphere. In a stationary process the density ρ of the neutrons within the layer is a function of the radius r alone and for our purpose sufficiently well described by the equation

$$d^2(r\rho)/dr^2 + 3f/\lambda^2 \cdot (r\rho) = 0$$

where λ is the mean free path of the neutrons for nuclear collisions in the layer and f is the fraction of the nuclear collisions that yields an additional neutron. This equation holds in the case of spherical symmetry ~~under assumptions which~~ if λ/r and f are both sufficiently small within the layer.

If r_2 is the outer radius of the spherical layer and r_1 its inner radius, stationary solutions are possible if the thickness of the layer $r_2 - r_1$ does not exceed a certain critical value $L(\lambda, f)$. The number of neutrons radiated into space from the outer surface tends to become infinite if the thickness of the layer approaches the critical thickness. If ~~we exceed~~ the critical thickness is exceeded no stationary solution is possible, and a neutron source can bring about an explosion.

Suggested Experiment.

For small $\frac{\lambda^2}{3f^2}$ and if the neutrons can freely escape from the outer surface of the layer ~~the value of the~~ ^{we get} ~~critical thickness L is~~ $L = \frac{\pi}{2\sqrt{3}f} \lambda$. For $\lambda = 10$ cm and $f = 1/100$ the critical thickness is of the order of magnitude of 100 cm.

Suggested Experiment.

It can be determined by ~~an~~ simple experiments ~~on a small scale~~ whether a given material is able to increase the number or energy of the neutrons by scattering neutrons in a layer of this material of a few centimetres' thickness. The elastic scattering causes some difficulty as it may hide the "non-elastic" effect in which we are interested. If, however, we surround a neutron source, the emission of which has spherical symmetry, by a spherical layer of the scattering material, the elastic scattering in the layer will not upset the spherical symmetry and will, therefore, not affect the total number of neutrons going through some point outside the layer. By measuring the total number of neutrons going through ~~some~~ some such point and comparing ^{layer} the value in the presence of the scattering/~~material~~ and in its absence we could see if neutrons are liberated or absorbed in the ~~layer~~ scattering material. Yet the elastic scattering affects the angular distribution of the neutrons going through any point which is close to the scattering layer, and can therefore make it difficult to interpret the measurements.

We could make use of the Fermi effect for measuring intensities of neutron beams i.e. we could measure the activity induced by neutrons in bodies formed of Fermi-active elements and draw conclusions on the number and energies of the neutrons to which these bodies have been exposed. Yet if we use sheets of the Fermi-active elements which we place close to the scattering layer in our experiment, the elastic scattering by affecting the angular distribution of the neutrons will affect the induced activity. (If ^{may be necessary} ~~we place these sheets at~~)

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 a great distance from the scattering layer we may not be
 able to get an induced activity which ^{will} yield in an
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 this difficulty can be removed by using a large number of
 small spheres of the Fermi-active element ~~and by using them in~~
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 It will also be possible to detect changes in the ing layer
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 neutrons by measuring the ratio of the Fermi-activity induced
 in several elements. We have theoretical evidence in favour
 of the forecast that for those heavier elements which have a
 Fermi effect of the neutron - proton or the neutron - alpha
 particle type, the activity induced by slow neutrons will
 strongly increase with increasing neutron energies. An
 investigation of the non-elastic scattering of elements like
 iodine which transmute into its own radioactive isotopes
 under neutron bombardment

A systematic investigation of the non-elastic
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 points of view; ^{for instance} it would throw light on the primary process
 involved in the Fermi effect of iodine and other elements
 which transmute into their own isotopes. Should it lead
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 Investigations along these lines will be started if the
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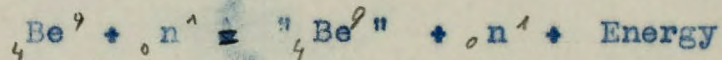
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Suggested Experiment.
~~XXXXXXXXXXXXXXXXXXXX~~

For small $\frac{\lambda^2}{3f^2}$ and if the neutrons can freely escape from the outer surface of ~~the layer~~ ^{we get} the value of the ~~critical thickness L is~~ $L = \frac{\pi \lambda}{2\sqrt{3f}}$. For $\lambda = 10$ cm and $f = 1/100$ the critical thickness is of the order of magnitude of 100 cm.

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points of view; *for instance* it would throw light on the primary process
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applications of far-reaching consequences would result.
Investigations along these lines will be started if the
necessary facilities can be obtained.

It is possible to use the Fermi effect as an indicator for the detection of neutron radiations. This may prove to be of special value for the investigation of neutron radiations in the presence of a strong gamma radiation. One might expect that even slow neutrons will induce radioactivity in elements which like iodine transmute in the Fermi effect into their own radioactive isotope, but further experiments are necessary to settle this point. Meanwhile T.A. Chalmers of St. Bartholomews Hospital and I worked out a method of isotopic separation which makes it possible to concentrate chemically the activity in the case of iodine and other elements which show a Fermi effect of this type. We used this method of isotopic separation to search for new neutron sources. By irradiating 25 grams of beryllium with the penetrating radiation from 150 mgms radium and exposing 100 cc. ethyl iodide to the radiation excited in the beryllium we could induce radioactivity in iodine, and separate chemically the radioiodine from the ethyl iodide in the form of a silver iodide precipitate. This precipitate showed a strong activity decaying with a period of 30 minutes, the initial activity being more than 15 times stronger in the presence of beryllium than in its absence. About half of the residual activity in the control experiment may be due to neutrons coming direct from the radium source, the other half represents the natural background effect of the counter. Apparently the gamma rays of radium liberate neutrons from beryllium which induce a strong Fermi effect in iodine. The 30 minutes and the six hours half periods of bromine can also be strongly excited by these neutrons as we have seen in co-operation with E. Glückauf. I was very much interested to hear just now that Professor McLennan has repeated some of our experiments and was able to confirm our results.

If we determine which elements show a Fermi effect when exposed to neutrons from a gamma ray disintegration we get by means of very simple experiments some information both regarding both the processes involved in the Fermi effects and in the gamma ray disintegration. By using the Fermi effects one could thus supplement in some respects the method of Chadwick and Goldhaber who were the first to detect a gamma ray disintegration in their pioneer work on heavy hydrogen. I wish to take this opportunity to mention that this work has been carried out in the Physics Department of St. Bartholomews Hospital and was made possible by the very kind co-operation of Professor Hopwood.

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Nuclear chain reactions and the possibility of an active power balance in transmutation processes

Sir,

I wish to draw attention to ~~a special class~~ ^{theoretically possible} that belong to a special class/ ~~simple~~ ^{simple} of transmutation processes/and indicate/experiments for their detection by which it could be determined if such processes can be maintained in one of the existing

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If an element is bombarded by protons or other positive nuclei ~~the~~ the vast majority of the moving particles are ~~is~~ stopped before they have had a chance to cause transmutation. This does not hold for bombardment with neutrons; one might think however, that the inefficiency ~~will~~ of their generation would rule out the possibility of an active power balance. Being aware (for the past twelve months) that we can escape such a conclusion if we succeed in maintaining processes in which collisions ^{of neutrons} leading to transmutation do not stop the neutrons from/ ^{further} remaining active/ ^{in the process} but increased ^{average} their energy or ~~their~~ number, I gave some thought to the main types of theoretically possible "chain reactions". ~~Neutrons of the mass number~~ ^{Since} ~~number~~ (There is no conclusive evidence as yet showing that neutrons of the mass number two, ^{or} negative protons, ^{etc.} or ~~diplons~~, or other non-positive nuclei which could serve as links in such chains have been actually generated in the laboratory. Therefore ^{for the present} it is sufficient to point out

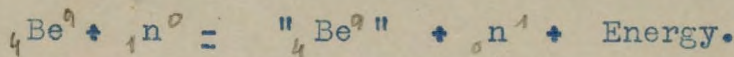
for the present that a chain reaction in which only one kind of non-positive nucleus/^{for instance the neutron (n^1)} forms the links of the chain must necessarily involve a metastable element ^{whereas if} ~~if~~

two different kinds of non-positive nuclei form the links it is theoretically ^{stable} possible to maintain chains in ~~a~~ mixtures of ~~certain~~ elements and perhaps also in certain pure elements ~~xxxx elements or in mixtures of elements/without involving~~ a metastable element. ^{stable}

^(n^1)
~~For pure neutron/chains we are limited to~~ elements of that class. ~~Apart from Uran and other radio-~~ active elements which betray their metastable character

~~but there is reason to think that~~ by their activity we know Beryllium to be metastable. ~~there are now radi metastable elements~~
Its mass, ^(The mass of Be) as often pointed out, is sufficient to ~~allow~~

permit a spontaneous disintegration into two alpha particles and a neutron. We do not know why such disintegration is inhibited and some sort of transmutation may be made possible in a nuclear collision. ^{with a neutron} A neutron hitting a Beryllium nucleus would then liberate energy without getting captured and could go on hitting/efficiently further Beryllium nuclei, the total number of its efficient collisions and the total amount of the liberated energy being determined by the geometrical conditions: ~~a reaction of this type~~



"Be" would be an isomer of Be, which would or would not break up into parts.

Additional neutrons could be liberated along ^(some) such a chain ^{some definite} in a certain fraction (f) of the nuclear collisions ^{in which that occurs} ($f < 1$). ^{and chains} ~~Stability Conditions.~~ ^{will be referred to as} ~~Stability Conditions.~~ ^{get a rough} ~~what idea about the geometrical conditions~~

We wish to consider as an example a closed spherical layer and assume that a neutron chain is maintained within the layer by a neutron source placed in the centre of the hollow sphere. The density ρ of the neutron within the layer between the inner radius r and the outer radius r_2 will be given as a function of the radius r by ^{the}

~~equation~~

*among
which are not
radioactive
element*

$$d(rp)/dr + 3f/\lambda^2 \rho = 0$$

where λ is the mean free path of the neutrons in the layer for elastic collisions. This equation holds in the case of spherical symmetry and yields the right order of

which may be realized
suff. closely ~~magnitudes~~ *if the inner radius of the hollow sphere (r = r₁) is large enough as compared to λ , and the fraction of*

neutrons if ~~the collisions which yield an additional neutron (f) are small as compared to 1.~~ *sufficiently* If we assume that the neutrons

can escape freely into a space from the outer surface (r = r₂). *number of* the ratio of the neutrons radiated into space to the neutrons emitted by the neutron source in the centre of the sphere tends to become infinite, if the thickness of the sheet (r₂ - r₁) approaches a critical value l(r₁).

number of
which ~~We find~~ *the smaller value holding for large r₁.* *approaches zero*
 $\frac{dp}{dr} < l <$

being the limit If (r₂ - r₁) exceeds the critical value we get an explosion.

For $\lambda = 10$ cm, $f = 1/100$ and large r₁ the critical thickness would be 85 cm. The thickness required for doubling the number of neutrons is about two thirds of the critical thickness.

~~xSuggested Experiment.~~ Radio-Activity induced by Neutrons.

the In order to ~~determine~~ test for a substance its capacity of increasing the energy or the number of the neutrons which are scattered in it in an experiment on a small scale, it may be convenient to use radio-activity induced by neutrons *for measuring neutron in hospitals* as an indicator. This would make it possible to carry out such experiments *by means* at any place where ordinary counters are available *from* ~~provided if~~ radon is supplied from some hospital. *source*

One must not think that because the neutron carries no positive charge the coulomb field of the nucleus cannot prevent processes in which the neutron disappears, a proton appearing instead of the neutron and leaving a

If we surround a neutron source with a closed layer of a material, in which a chain re-action is maintained by the neutron radiation of the source we can theoretically liberate an unlimited amount of energy; ~~and if additional neutrons are liberated along the chain we can also obtain an unlimited number of neutrons liberated by some definite number of neutrons emitted by the source.~~ *if this layer is sufficiently thick and multiplying if we have had a chain* In order to get a rough idea of the geometrical conditions ~~in which a stationary process is possible in the latter case including~~ *is necessary* the order of magnitude of the linear dimensions involved, ~~we shall make some assumptions which will simplify the~~ *process in a multiplying chain* problem without changing its essential characteristics, and make use of the differential equation which will supply a fairly good description of the process.

We consider *a multiplying chain* a closed spherical layer in which a neutron chain is maintained by a neutron source placed in the centre of the hollow sphere. ~~If the neutrons can escape freely into space from the outer surface (r = r₂) of the spherical layer the density of the neutrons within the layer will be zero for r = r₂.~~ *is sufficiently small for our purpose and will* This density is described within the layer by the equation

$$d(r^2 \rho) / dr + 3f / \lambda \cdot \rho = 0$$

where λ is the mean free path of the neutrons for nuclear collisions in the layer and f is the fraction of the nuclear collisions that yield an additional neutron. This equation holds in the case of spherical symmetry under assumptions which may be sufficiently closely realised if λ / r and f are both sufficiently small, *in the layer.* ~~if the neutrons can escape freely into space~~

The ratio of the number of neutrons radiated into space from the outer surface (r = r₂) to the number of neutrons emitted by the neutron source in the centre of the sphere *and entering the inner surface of the layer (r = r₁)* is given by the ~~ratio~~ ratio of the values of

for r = r₂ and r = r₁. This ratio tends to become infinite if *dρ/dr* approaches zero *for r = r₁* and this occurs for a certain X

nature of the material thickness:
 of the neutrons can escape freely into space from the outer surface we have $\rho(r_2) = 0$ and set for the critical thickness $\rho(r_1) = 0$

radio-active element is formed which ^{subsequently} transmutes into the original element. ~~One should not expect~~ The energy of the proton ~~is~~ ^{is in such a process necessarily} smaller than the energy of the neutron. One should not expect that such a process ^{would} take place unless the energy of the ejected proton is sufficient to enable it to penetrate near to the nucleus against the Coulomb field in the inverse process. It should therefore be surprising if slow neutrons could induce such ^{or similar} processes in sufficiently heavy elements (and ^{equally} also if they could induce processes in which an alpha particle ~~plays the role~~ ^{instead} of the proton, though the energy of the alpha particle can exceed the energy of the neutron), and if further experiments will confirm our expectation we could estimate a change in the energy of a neutron beam by ^{comparing} ~~measuring~~ the ~~induced~~ activity induced in ^{certain} elements of different atomic number.

Suggested Experiment.

If one wishes to test the efficiency of some ~~in order~~ scattering material one has to face the difficulty that the elastic scattering may hide the "inelastic" effect in which we are interested. If we surround a neutron source the emission of which has spherical symmetry, by a spherical layer of the test material the elastic scattering in the layer will not upset the spherical symmetry and will therefore not affect the total number of neutrons going through any point outside the layer. By measuring the total number of neutrons going through such a given point and comparing the value ^{in the presence of} ~~with and without~~ the test material and without ^{in its} it we could, theoretically at least, obtain useful information. Yet the elastic scattering ^{greatly} affects the angular distribution of the neutrons going through any point which is close to the layer and would therefore affect the activity induced in a sheet of ^{some suitable} susceptible material placed close to the layer, which we may wish to use ^{if this such a sheet} as a probe close to the layer we know in ^{advance} its intensity.

~~as indicator.~~

Replacing this ^{such a} sheet by a large number

of small spheres seems to be the adequate solution of this

difficulty; ^{since} in view of the fact that we cannot afford

to lose ~~much~~ intensity ^{by choosing a large distance between} if we wish to observe a change

of about 1% in the number or mean energy of the neutrons

and have to use a neutron source which is based on ^{activated by boron} radon.

In view of ^(consequences possibly implications) the possible implications for our

civilisation of ^{by a systematic measurement} measurement of the inelastic scattering

of neutrons in ^{metastable} metastable elements, ^{and} I felt I had better

not hesitate any longer in raising this subject, since

I am not certain whether I shall have an opportunity to

carry out such experiments myself.

~~In view of the ^{possible} implications~~

~~L. A. Langere Fassang~~

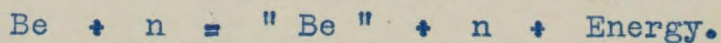
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I wish to draw attention to the theoretically possible transmutation processes of a special type and indicate simple experiments which could lead to their detection. The energy liberated in a process of this type may very well be large as compared to the energy input required for the maintenance of the process, and if ~~it~~ ^{such a process} ~~is~~ ^{can} used for the generation of power we may have an active ^{be realized} power balance. ^{and}

^{for instance for instance} By radiating a metastable element with neutrons it may prove to be possible to maintain a process in which collisions of neutrons ^{by colliding with} with nuclei of the metastable element ^{caused by their collisions} lead to a transmutation of the latter which ^{is not} does not stop the neutron from further remaining active ^{and} in the process ^{and} but increases ^{their} the average energy of number ^{and} of the neutrons. ^{we may have a nuclear chain reaction}

^{It is believed} We have reason to believe that there exist metastable elements apart from those elements which betray their metastable character by their radio-activity, ^{seems to be} The mass of Beryllium ^(for instance) is ~~is~~ sufficient to allow its spontaneous disintegration, into two alpha particles and a neutron, which is apparently inhibited under ordinary conditions.

Such inhibition may, however, be lifted in a nuclear collision with a neutron; a neutron hitting a Beryllium nucleus would then liberate energy without getting captured and could go on hitting efficiently further Beryllium nuclei, the total number of its efficient collisions, and the total amount of the liberated energy being determined by the geometrical conditions ^{only}. ^{We shall call a reaction of this type a "chain"}



"Be" would be an isomer of Be, which would or would not break up into parts.

Additional neutrons could be liberated along some such chains, which will then be called ^{divergent} multiplicative chains in this note.

A metastable element must necessarily be non-positive involved in a chain in which only one kind of ~~particular~~ nucleus, for instance only ~~the~~ neutrons, form the links of the chain. (single chain)

It is theoretically possible to maintain chains in mixtures of stable elements and also in certain pure stable elements if two different kinds of non-positive nuclei form the links of the chain. (double chain) ~~the same element~~ ~~kindly~~

~~as yet showing that negative protons or neutrons of the mass number two, which could, together with the neutron, serve as links in such chains) have been actually generated in the laboratory.~~ ~~some progress~~ ~~the discovery of~~ ~~nuclei chains~~ ~~shall be postponed.~~

Stationary divergent chains.

If we surround a neutron source with a closed layer of a material in which a chain reaction is maintained by the source we can theoretically liberate an unlimited amount of energy and in the case of a divergent chain also an unlimited number of neutrons. ~~We wish~~ ~~in order to get~~

~~Some idea of the geometrical conditions in which a stationary process can be maintained for a divergent chain of orders of magnitudes involved, we wish to consider a closed spherical layer in which such a chain is maintained by~~ ~~and an~~ ~~can be obtained by we~~ ~~therefore~~ ~~ing~~

In a stationary process within the layer the density ρ of the neutrons is sufficiently well described for our purpose as a function of the radius r by the equation

$$d(r\rho)/dr + 3f/(r\lambda) = 0$$

$$\frac{3f}{2}(r\rho)$$

where λ is the mean free path of the neutrons for nuclear collisions in the layer and f is the fraction of the nuclear collisions that yield an additional neutron. This equation holds in the case of spherical symmetry under assumptions which may be sufficiently closely realised if λ/r and f are both sufficiently small within the layer.

If r_2 is the outer radius of the spherical layer and r_1 its inner radius, stationary solutions are possible if the thickness of the layer $r_2 - r_1$ does not exceed a certain

critical value. If the neutrons can freely escape from the outer surface $r = r_0$, the value l of the critical thickness ~~is for large~~ ^{is a small} ~~values of λ~~ ^{values of λ}

For $\lambda = 10$ cm and $f = 1/100$ we get for instance l of the order of magnitude ^{of} 100 cm.

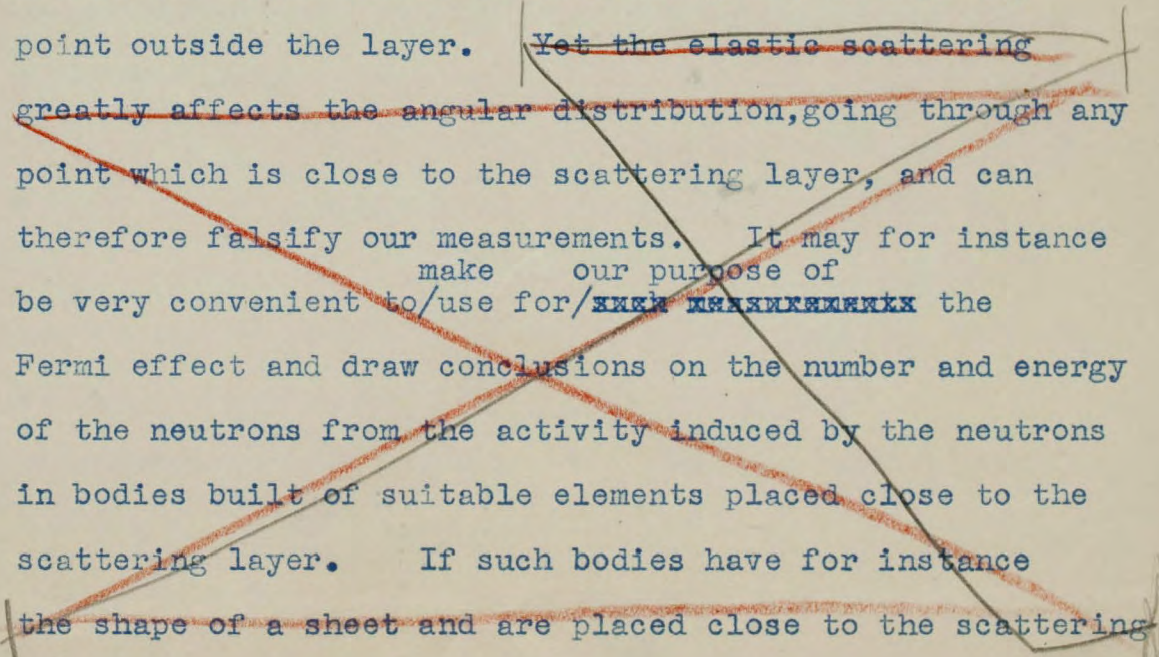
The number of neutrons radiated into space from the outer surface tends to be come infinite if the thickness of the layer approaches the critical thickness. If we exceed the critical thickness no stationary solution is possible and we would get an explosion. (At about ^{however} ~~2/3 of the critical thickness~~ the number of the neutrons radiated by the source ^{in the volume} is only doubled by the chain reaction.)

Suggested Experiment.

It would be possible to detect for any given material whether it is able to increase the energy or number of the neutrons by experiments ^{on a small scale} in which the neutrons are scattered ^{by a layer of a few centimeter thickness} in the test material. The elastic scattering ^{of this material} in the material causes some difficulty as it may hide the "inelastic" effect in which we are interested. If, however, we surround a neutron source, the emission of which has spherical symmetry, by a spherical layer of the test material, ^{this instance of a few cm thickness} the elastic scattering in the layer will not upset the spherical symmetry and will, therefore, not affect the total number of neutrons going through any point outside the layer. ~~Yet the elastic scattering greatly affects the angular distribution, going through any point which is close to the scattering layer, and can therefore falsify our measurements. It may for instance be very convenient to use for ~~such measurements~~ the Fermi effect and draw conclusions on the number and energy of the neutrons from the activity induced by the neutrons in bodies built of suitable elements placed close to the scattering layer. If such bodies have for instance the shape of a sheet and are placed close to the scattering~~

not -
of this material

by scattering
neutrons
in a layer
of a few
cm thickness
of this mate-
rial.



By measuring the total number of neutrons going through such a given point and comparing the value in the presence of the test material and in its absence we could ^{see if} ~~theoretically at least~~ obtain useful information. Yet

the elastic scattering greatly affects the angular distribution, ^{of the intensity in} ~~going through any point~~ which is close to the scattering layer, and can therefore, ^{make the} ~~in practice, falsify our~~ measurements. ^{it is difficult to carry out the measurement}

^{We could} ~~It may for instance be very convenient to make use for our purpose of the Fermi effect, and i.e. to~~ ^{measure the activity induced by the neutrons in} ~~bodies~~ ^{built of} ~~suitable elements~~ ~~mixed with the scattering~~

~~XXXX~~ and draw conclusions on the number and energy of the neutrons ^{which have gone} ~~going through these bodies.~~ Yet if such ^{of the Fermi alpha elements} ~~bodies have the shape of a sheet, and are placed close~~ ^{in our experiment} to the scattering layer (~~xx xx~~ and it may be necessary

to place them close to the layer in order to induce an activity that will yield a large number of impulses - in an electron counter, sufficiently large to detect changes of 1% in the energy or number of the neutrons),

the elastic scattering by affecting the ^{mentioned} angular distribution ^{of the neutrons} will greatly affect the observed induced activity. ^{Fortunately this} This difficulty can be removed by using

a large number of small spheres of the material which is to be activated and ^{replacing} ~~replaced~~ by them, the above-mentioned sheet.

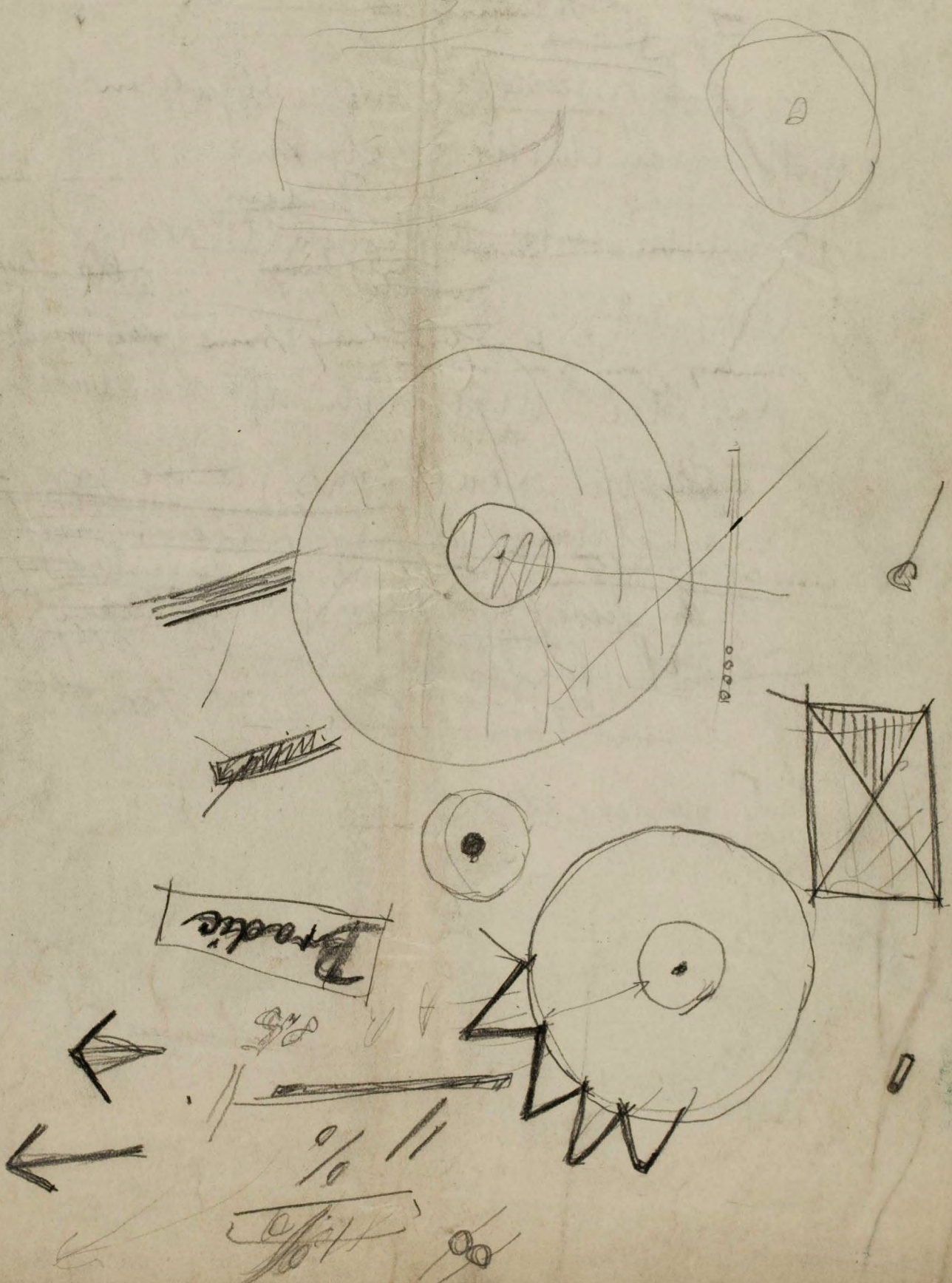
^{We have} ~~There is very strong~~ theoretical evidence in favour of the ^{present} ~~assumption~~ that ^{for those} ~~some of the heavier~~ elements which have a Fermi effect of a certain type, the activity induced by slow neutrons will strongly increase with increasing neutron energies. This ^{will} would make it possible to detect a change ⁱⁿ ~~in~~ the neutron energy by measuring the ratio of the activity induced in several elements.

^a ~~The expense involved in a systematic investigation of the "inelastic" scattering of the elements is small. Both in its cost and in its complexity. The ratio of the cross-sections is not too small, deriving from it if it yields~~

- 5 -

NON-

A systematic investigation of the elastic behavior
of the elements would be of expansive value. Material
for a cyclic chain reaction were to be found thereby
the ratio of the immediate economic value of the proposed
investigation to its expense would exceed 10.



On Nuclear Chain Reactions and their Bearing on the Question
of Power Production.

Sir,

I wish to draw attention to ~~the~~ theoretically possible transmutation processes of a special type and indicate simple experiments which could lead to their detection. The energy liberated in a process of this type may very well be large as compared to the energy input required for the maintenance of the process; if such a process can be realised and is used for the generation of power we may therefore have an active power balance. For instance by radiating a metastable element with neutrons it may prove to be possible to maintain a process in which neutrons cause a metastable element to transmute without being stopped from further remaining active in the process and increasing their average energy and number i.e. we may have a nuclear chain reaction. It is believed

Sir,

I wish to draw attention to the theoretically possible transmutation processes of a special type and indicate simple experiments which could lead to their detection. The energy liberated in a process of this type may very well be large as compared to the energy input required for the maintenance of the process, and if it is used for the generation of power we may have an active power balance. By radiating a metastable element with neutrons it may prove to be possible to maintain a process in which collisions of neutrons with nuclei of the metastable element lead to a transmutation of the latter which does not stop the neutron from further remaining active in the process but increases the average energy of number of the neutrons.

We have reason to believe that there exist metastable elements apart from those elements which betray their metastable character by their radio-activity, ^{seems to be} The mass of Beryllium/~~is~~ even sufficient to allow its spontaneous disintegration into two alpha particles and a neutron, which is apparently inhibited under ordinary conditions. Such inhibition may, however, be lifted in a nuclear collision with a neutron; a neutron hitting a Beryllium nucleus would then liberate energy without getting captured and could go on hitting efficiently further Beryllium nuclei, the total number of its efficient collisions, and the total amount of the liberated energy being determined by the geometrical conditions only.



"Be" would be an isomer of Be, which would or would not break up into parts.

Additional neutrons could be liberated along some such chains, which will then be called multiplicative chains in this note.

A metastable element must necessarily be involved in a chain in which only one kind of ^{non-positive} ~~positive~~ nucleus for instance only neutrons form the links of the chain.

It is theoretically possible to maintain chains in mixtures of stable elements and also in certain pure stable elements if two different kinds of non-positive nuclei form the links of the chain, but there is no conclusive evidence as yet showing that negative protons or neutrons of the mass number two which could, together with the neutron, serve as links in such chains have been actually generated in the laboratory.

If we surround a neutron source with a closed layer of a material in which a chain reaction is maintained by the source we can theoretically liberate an unlimited amount of energy and in the case of a divergent chain also an unlimited number of neutrons. In order to get some idea of the geometrical conditions in which a stationary ^{and} process can be maintained for a divergent chain/ of the orders of magnitudes involved we wish to consider a closed spherical layer in which such a chain is maintained by a neutron source placed in the centre of the hollow sphere. In a stationary process within the layer /The density of the neutrons/ is sufficiently well described for our purpose as a function of the radius r by the equation

$$d(r)/dr + 3f/l = 0$$

where l is the mean free path of the neutrons for nuclear collisions in the layer and f is the fraction of the nuclear collisions that yield an additional neutron. This equation holds in the case of spherical symmetry under assumptions which may be sufficiently closely realised if l/r and f are both sufficiently small/ ^{within} the layer.

If r is the outer radius of the spherical layer and r' its inner radius, stationary solutions are possible if the thickness of the layer $r - r'$ does not exceed a certain

critical value. If the neutrons can freely escape from the outer surface $r = R$ the value l of the critical thickness is for large r close to

$$l = \dots$$

For $R = 10$ cm and $f = 1/100$ we get for instance l of the order of magnitude 100 cm.

The number of neutrons radiated into space from the outer surface tends to become infinite if the thickness of the layer approaches the critical thickness. If we exceed the critical thickness no stationary solution is possible and we would get an explosion. At about $2/3$ of the critical thickness the number of the neutrons radiated by the source is only doubled by the chain reaction.

Suggested Experiment.

It would be possible to detect for any given material whether it is able to increase the energy or number of the neutrons by experiments in which the neutrons are scattered in the test material. The elastic scattering in the material causes some difficulty as it may hide the "inelastic" effect in which we are interested. If, however, we surround a neutron source the emission of which has spherical symmetry, by a spherical layer of the test material the elastic scattering in the layer will not upset the spherical symmetry and will, therefore, not affect the total number of neutrons going through any point outside the layer. Yet the elastic scattering greatly affects the angular distribution, going through any point which is close to the scattering layer, and can therefore falsify our measurements. It may for instance be very convenient to use for ~~such~~ ~~purposes~~ the Fermi effect and draw conclusions on the number and energy of the neutrons from the activity induced by the neutrons in bodies built of suitable elements placed close to the scattering layer. If such bodies have for instance the shape of a sheet and are placed close to the scattering

By measuring the total number of neutrons going through such a given point and comparing the value in the presence of the test material and in its absence we could theoretically at least obtain useful information. Yet the elastic scattering greatly affects the angular distribution, going through any point which is close to the scattering layer, and can therefore in practice falsify our measurements. It may for instance be very convenient to make use for our purpose of the Fermi effect, and measure the activity induced by the neutrons in bodies built of suitable elements ~~placed close to the scattering layer~~ and draw conclusions on the number and energy of the neutrons going through these bodies. Yet if such bodies have the shape of a sheet and are placed close to the scattering layer (~~in it~~ and it may be necessary to place them close to the layer in order to induce an activity that will yield a large number of impulses in an electron counter, sufficiently large to detect changes of 1% in the energy or number of the neutrons), the elastic scattering by affecting the mentioned angular distribution will greatly affect the observed induced activity. This difficulty can be removed by using a large number of small spheres of the material which is to be activated and replacing by them the above mentioned sheet.

There is very strong theoretical evidence in favour of the assumption that ^{for} some of the heavy elements which have a Fermi effect of a certain type the activity induced by slow neutrons will strongly increase with increasing neutron energy. This would make it possible to detect a change in the neutron energy by measuring the ratio of the activity induced in several elements.

A systematic investigation of the ^{non-}elastic scattering of the elements would not be expensive. If material for a suitable chain reaction were to be found thereby the ratio of the immediate economic value of the proposed investigation to its expense would exceed 10.

Lanyere Fessog.

Sir,

theoretically possible
I wish to draw attention to ~~a special class~~ simple
that belong to a special class/
~~of~~ transmutation processes/and indicate/experiments
for their detection
by which it could be determined if such processes
can be maintained in one of the existing

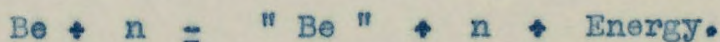
Sir,

I wish to draw attention to theoretically
possible transmutation processes ~~of a~~ of a
type
special ~~class~~/ and indicate simple experiments which
could lead to their detection. The energy liberated
in a process of this type may very well be large as
compared to the energy input required for ~~the~~ the maintenance
of the process i.e. we may have an active power balance.

If an element is bombarded by protons or other
positive nuclei ~~in~~ the vast majority of the moving particles
are
~~is~~/stopped before they have had a chance to cause trans-
mutation. This does not hold for bombardment with
neutrons; one might think however, that the inefficiency
~~would~~ of their generation would rule out the possibility
of an active power balance. Being aware for the past
twelve months that we can escape such a conclusion if
we succeed in maintaining processes in which collisions
leading to transmutation do not stop the neutrons ^{further} from/
~~remaining active~~ ^{in the process} but increased their energy or their
number I gave some thought to the main types of theoretical-
ly possible "chain reactions"; ~~There is no conclusive evidence as yet showing~~
~~that neutrons of the mass number two, negative protons~~
or diplotons or other non-positive nuclei which could serve
as links in such chains have been actually generated in
the laboratory. Therefore it is sufficient to point out

for the present that a chain reaction in which only one kind of non-positive nucleus/^{for instance the neutron (n)}forms the links of the chain must necessarily involve a metastable element. If two different kinds of non-positive nuclei form the links it is theoretically possible to maintain chains in a mixtures of certain elements and perhaps also in certain pure elements ~~pure elements or in mixtures of elements~~/without involving a metastable element.

(n)
For pure neutron/chains we are limited to elements of that class. Apart from Uran and other radioactive elements which betray their metastable character by their activity we know Beryllium to be metastable. Its mass, as often pointed out, is sufficient to ~~allow~~ permit a spontaneous disintegration into two alpha particles and a neutron. We do not know why such disintegration is inhibited and some sort of transmutation may be made possible in a nuclear collision. A neutron heating a Beryllium nucleus would then liberate energy without getting captured and would go on hitting/^{efficiently}further Beryllium nuclei the total number of its efficient collisions and the total amount of the liberated energy being determined by the geometrical conditions.



"Be" would be an isomer of Be, which would or would not break up into parts.

Additional neutrons could be liberated along such a chain in a certain fraction (F) of the nuclear collisions (f l).

Stability Conditions.

We wish to consider as an example a closed spherical layer and assume that a neutron chain is maintained within the layer by a neutron source placed in the centre of the hollow sphere. The density of the neutron within the layer between the inner radius r and the outer radius R will be given as a function of the radius r by

$$d(r)/dr + 3f/\lambda = 0$$

Where λ is the mean free path of the neutrons in the layer for elastic collisions. This equation holds in the case of spherical symmetry and yields the right order of magnitudes in the inner radius of the hollow sphere ($r = r_1$) is large enough as compared to λ , and the fraction of the collisions which yield an additional neutron (f) small as compared to 1. If we assume that the neutrons can escape freely into a space from the outer surface ($r = r_2$) the ratio of the neutrons radiated into space to the neutrons emitted by the neutron source in the centre of the sphere tends to become infinite if the thickness of the sheet ($r_2 - r_1$) approaches a critical value $l(r)$.

We find

the smaller value holding for large r . If ($r_2 - r_1$) exceeds the critical value we get an explosion.

For $\lambda = 10$ cm, $f = 1/100$ and large r the critical thickness would be 30 cm. The thickness required for doubling the number of neutrons is about two thirds of the critical thickness.

*Suggested Experiment. Radio-Activity induced by Neutrons.

In order to ~~determine~~ test for a substance its capacity of increasing the energy or the number of the neutrons which are scattered in it in an experiment on a small scale it may be convenient to use radio-activity induced by neutrons as an indicator. This would make it possible to carry out such experiments at any place where ordinary counters are available ~~provided~~ if radon is supplied from some hospital.

One must not think that because the neutron carries no positive charge the coulomb field of the nucleus cannot prevent processes in which the neutron disappears, a proton appearing instead of the neutron and leaving a

radio-active element is formed which transmutes into the original element. ~~One should not expect~~ The energy of the proton ~~is~~ ^{is} smaller than the energy of the neutron. One should not expect that such a process takes place unless the energy of the ejected proton is sufficient to enable it to penetrate near to the nucleus against the Coulombe field in the inverse process. It should therefore be surprising ~~is~~ if slow neutrons could induce such processes in sufficiently heavy elements (and also if they could induce processes in which an alpha particle plays the role of the proton, though the energy of the ^{ejected} alpha particle can exceed the energy of the neutron), and if further experiments will confirm our expectation we could estimate a change in the energy ^{and abundance} of a neutron beam by ~~measuring~~ ^{comparing} the ~~induced~~ activity induced in elements of different atomic number.

Suggested Experiment.

~~If one wishes~~ ^{to test} the efficiency of some ~~in order~~ ^{different} scattering material one has to face the difficulty that the elastic scattering may hide the "inelastic" effect in which we are interested. If we surround a neutron source the emission of which has spherical symmetry, by a spherical layer of the test material the elastic scattering in the layer will not upset the spherical symmetry and will therefore not effect the total number of neutrons going through any point outside the layer. By measuring the total number of neutrons going through such a given point and comparing ^{in the presence of} the value ~~with~~ ^{the test material and without} it we could theoretically at least obtain useful information. Yet the elastic scattering affects the angular distribution of the neutrons going through any point which is close to the layer and would therefore affect the activity induced in a sheet of susceptible material placed close to the layer which we may wish to use

as indicator. Replacing this sheet by a large number of small spheres seems to be the adequate solution of this difficulty. In view of the fact that we cannot afford to lose much intensity if we wish to observe a change of about 1% in the number or mean energy of the neutrons and have to use a neutron source which is based on radon.

In view of the possible implications for our civilisation of measurement of the inelastic scattering of neutrons in metastable elements, I felt I had better not hesitate any longer in raising this subject, since I am not certain whether I shall have an opportunity to carry out such experiments myself.

If we surround a neutron source with a closed layer of a material in which a chain re-action is maintained by the neutron radiation of the source we can theoretically liberate an unlimited amount of energy; and if additional neutrons are liberated along the chain we can also obtain an unlimited number of neutrons liberated by some definite number of neutrons emitted by the source. In order to get a rough idea of the geometrical conditions in which a stationary process is possible in the latter case including the order of magnitude of the linear dimensions involved, we shall make some assumptions which will simplify the problem without changing its essential characteristics, and make use of the differential equation which will supply a fairly good description of the process.

We consider a closed spherical layer in which a neutron chain is maintained by a neutron source placed in the centre of the hollow sphere. If the neutrons can escape freely into space from the outer surface ($r = r_0$) of the spherical layer the density of the neutrons within the layer will be zero for $r = r_0$. This density is described within the layer by the equation

$$d(r)/dr + 3r/l + f = 0$$

where l is the mean free path of the neutrons for nuclear collisions in the layer and f is the fraction of the nuclear collisions that yield an additional neutron. This equation holds in the case of spherical symmetry under assumptions which may be sufficiently closely realised if l/r_0 and f are both sufficiently small. ~~if the number of neutrons radiated~~

~~into space from the outer surface~~ The ratio of the number of neutrons radiated into space from the outer surface $r = r_0$ to the number of neutrons emitted by the neutron source in the centre of the sphere is given by the ~~ratio~~ ratio of the values of

for $r = r_0$ and $r = 0$. This ratio tends to become infinite if l/r_0 approaches zero and this occurs for a certain